

gaia

# Metallicity dependence of Classical Cepheids Period-Luminosity relations and the extragalactic distance scale

V. Ripepi

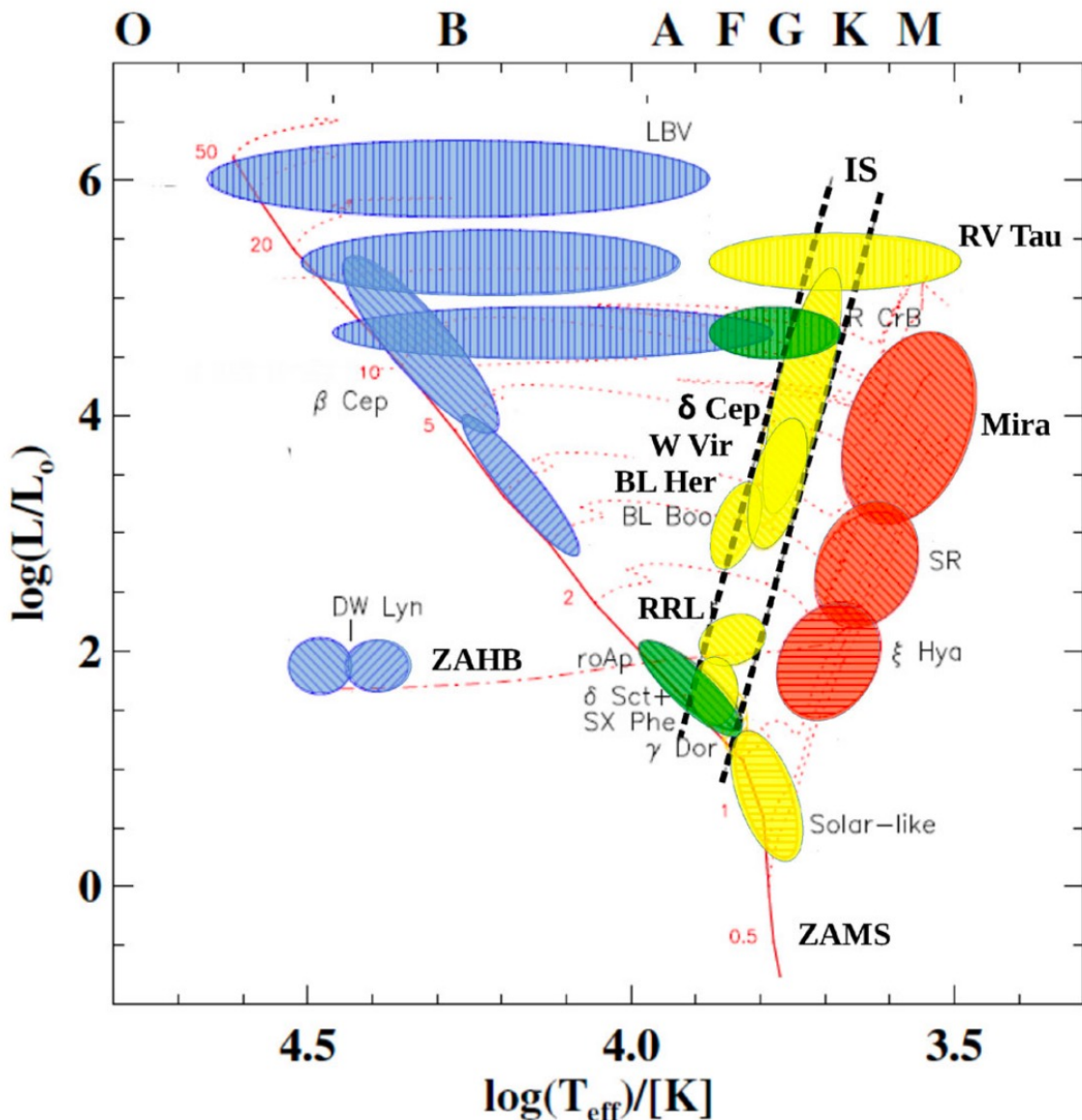
*INAF-Osservatorio Astronomico di Capodimonte*



# Outline

- Cepheid properties and their use
- Motivation for studying the metallicity dependence of the PLR
- C-MetaLL project
- Present baseline results
- Future improvement

# Classical Cepheid



## Classical Cepheids:

Central helium burning stars

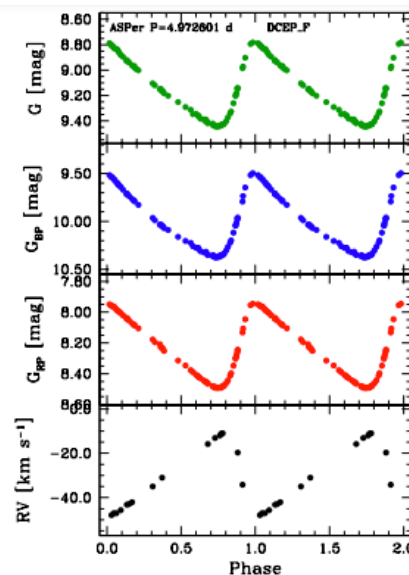
$M=3\div 13M_{\odot}$

$M_V = -2\div -7$  mag

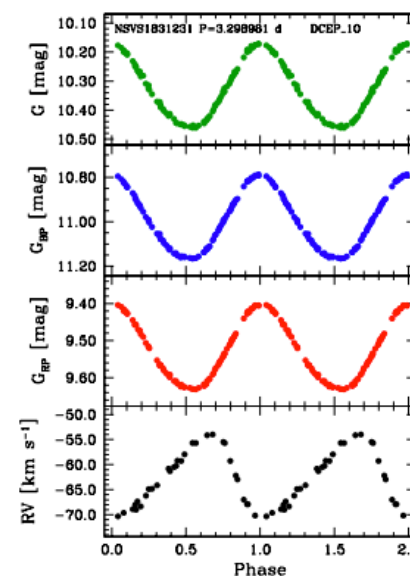
$P=0.2\div 100$  d

Ages: 50 $\div$ 500 Myrs

Pulsate in F, 1O, 2O, Multiple modes.



Fundamental



1<sup>st</sup> overtone

# Why Cepheids are important? The discovery of the period-luminosity relation

HARVARD COLLEGE OBSERVATORY.

CIRCULAR 173.

PERIODS OF 25 VARIABLE STARS IN THE SMALL MAGELLANIC CLOUD.

The following statement regarding the periods of 25 variable stars in the Small Magellanic Cloud has been prepared by Miss Leavitt.

Leavitt & Pickering (1912)



H. Leavitt

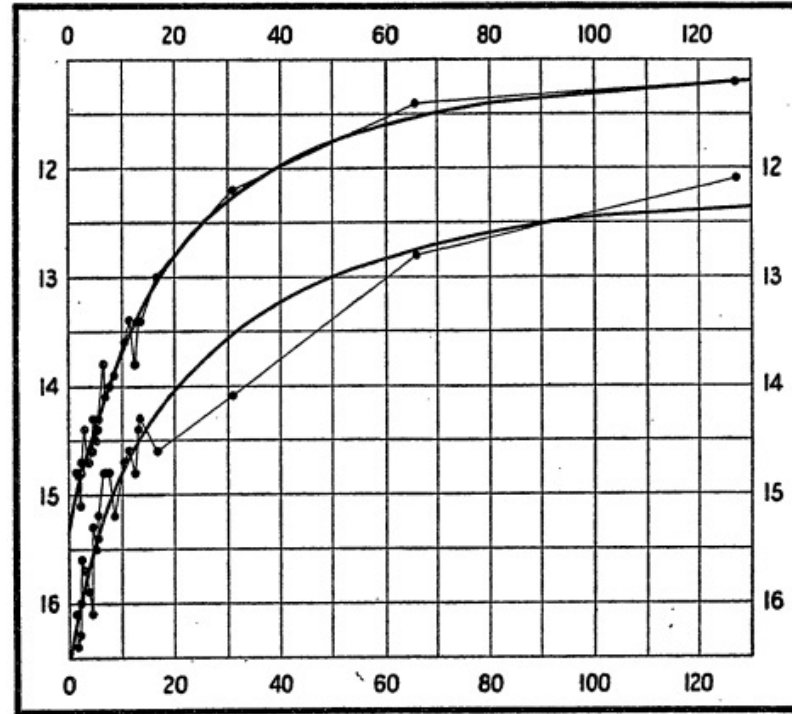


FIG. 1.

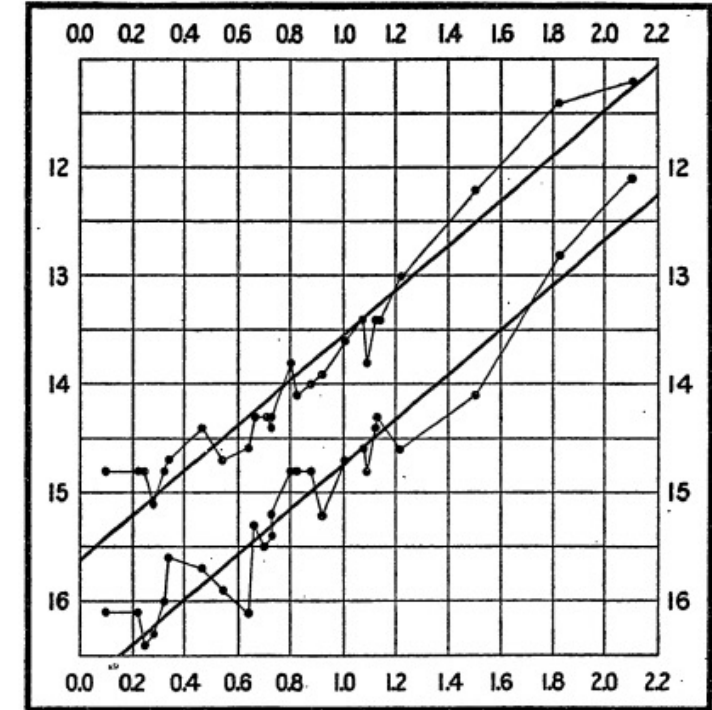


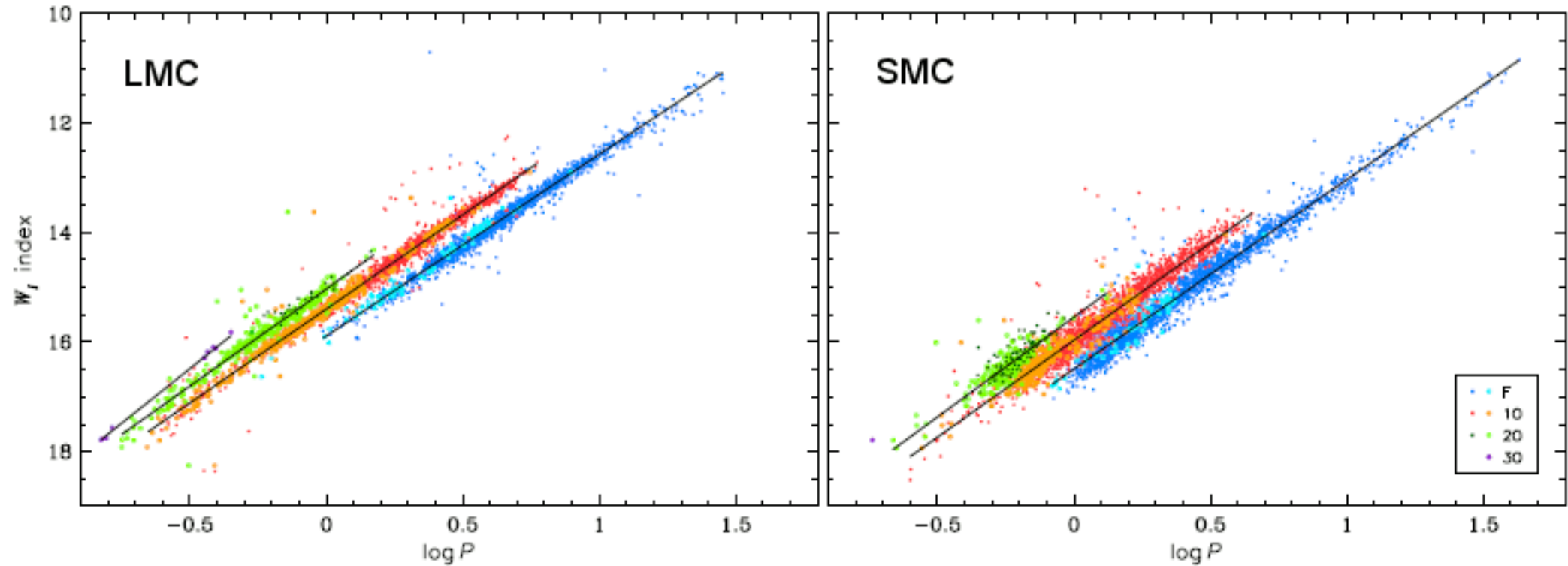
FIG. 2.

1. A straight line can readily be drawn among each of the two series of points corresponding to maxima and minima, thus showing that there is a simple relation between the brightness of the variables and their periods.

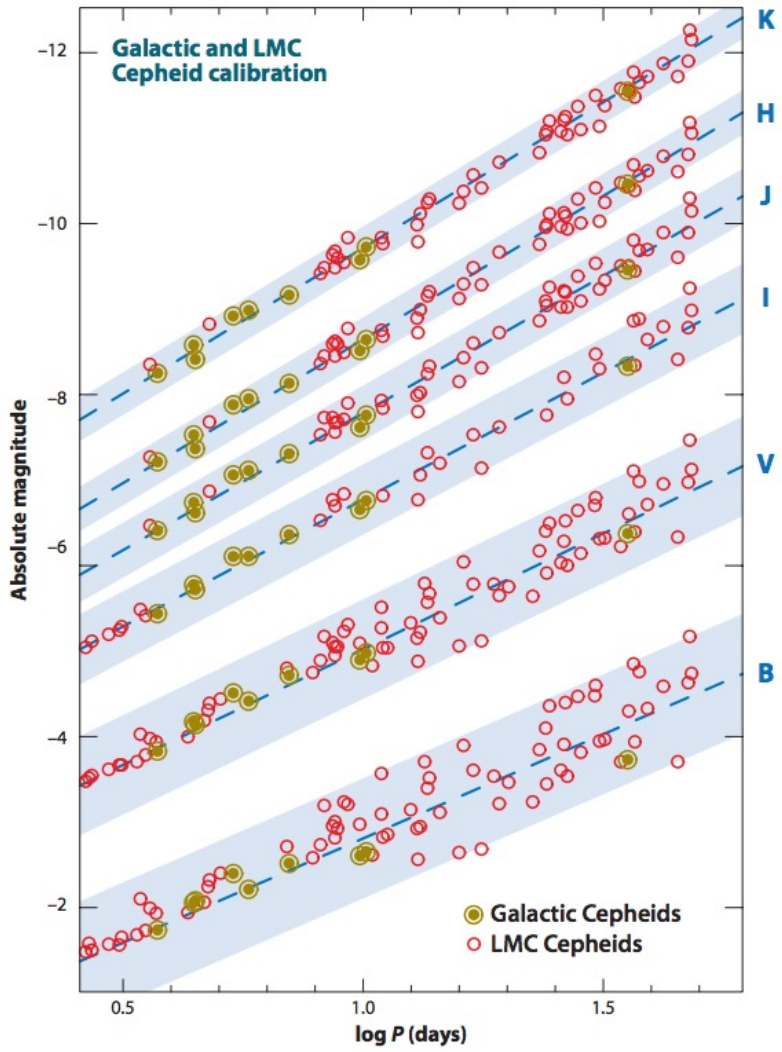


# Modern version of the Leavitt law

Tight PL relations in different modes

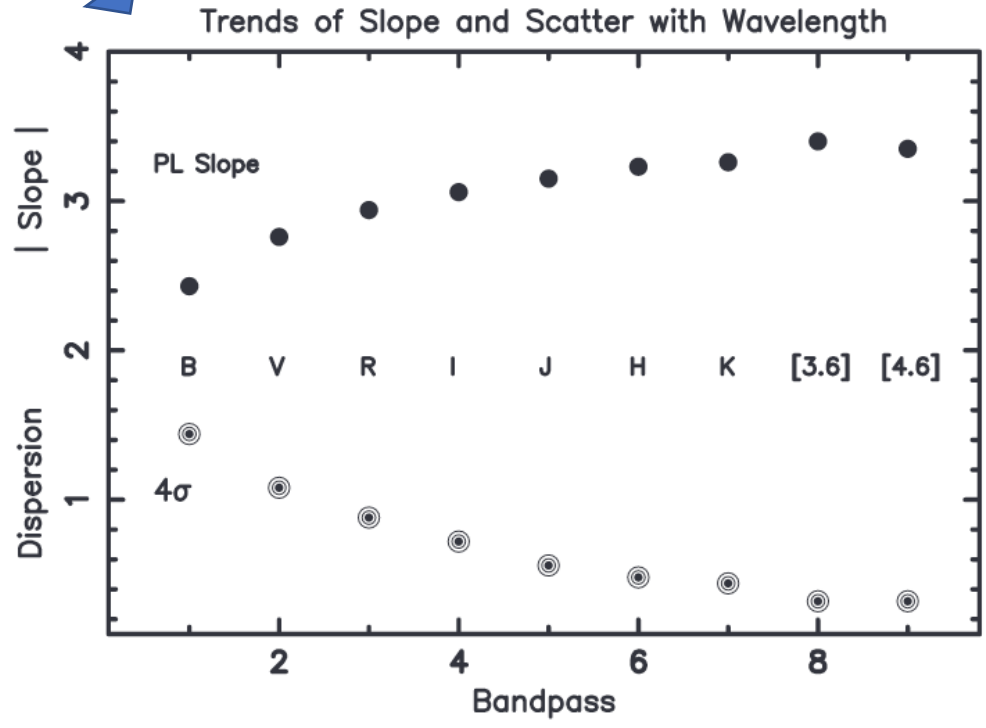
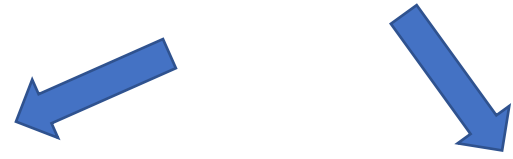


# Properties of the PL relations



Freedman & Madore (2010)

The slope of the Leavitt Law increases with increasing wavelength, with a corresponding decrease in dispersion.



Madore & Freedman (2012)

# The Wesenheit magnitudes

To bypass the reddening problem, in 1982 B. Madore introduced the so-called Wesenheit magnitudes  $W$  (Wesenheit is a German word meaning “essence”, “real nature”).

We adopt the V,I band as an example (any combination of magnitudes/colors can be used).

In this case, the ratio of total-to-selective absorption is  $R_{VI} = A_V / E(V - I)$ ,

$$W = V - R_{VI} \times (V - I), \quad (10)$$

as well as an intrinsic Wesenheit magnitude,  $W_o$ :

$$W_o = V_o - R_{VI} \times (V - I)_o. \quad (11)$$

By construction,

$$W = V_o + A_V - R_{VI} \times (V - I)_o - R_{VI} \times E(V - I) \quad (12)$$

$$= V_o - R_{VI}(V - I)_o + A_V - R_{VI} \times E(V - I), \quad (13)$$

where  $V = V_o + A_V$  and  $(V - I) = (V - I)_o + E(V - I)$ , and  $A_V = R_{VI} \times E(V - I)$ , thereby reducing the last two terms to zero, leaving  $W = V_o - R_{VI} \times (V - I)_o$ , which is equivalent to the definition of  $W_o$ .

**Wesenheit magnitudes are reddening free ! → huge reduction of the uncertainty on the measure of  $H_0$**

**Particularly important the Wesenheit magnitude in the HST filters used by the SH0ES team to estimate  $H_0$ :  $W_{\text{HST}} = \text{F160W (H)} - 0.386 (\text{F555W (V)} - \text{F814W (I)})$**

# Classical Cepheids are Standard Candles (term introduced by H. Leavitt)

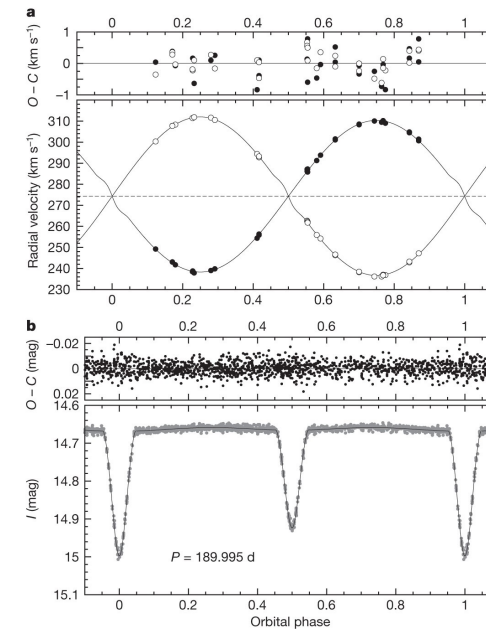
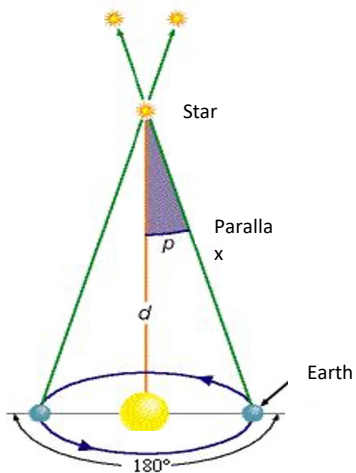
- Astronomical objects whose intrinsic brightness (absolute magnitude) is known → distance !

$$m - M = -5 + 5 \log_{10} D \quad (D \text{ in parsec})$$

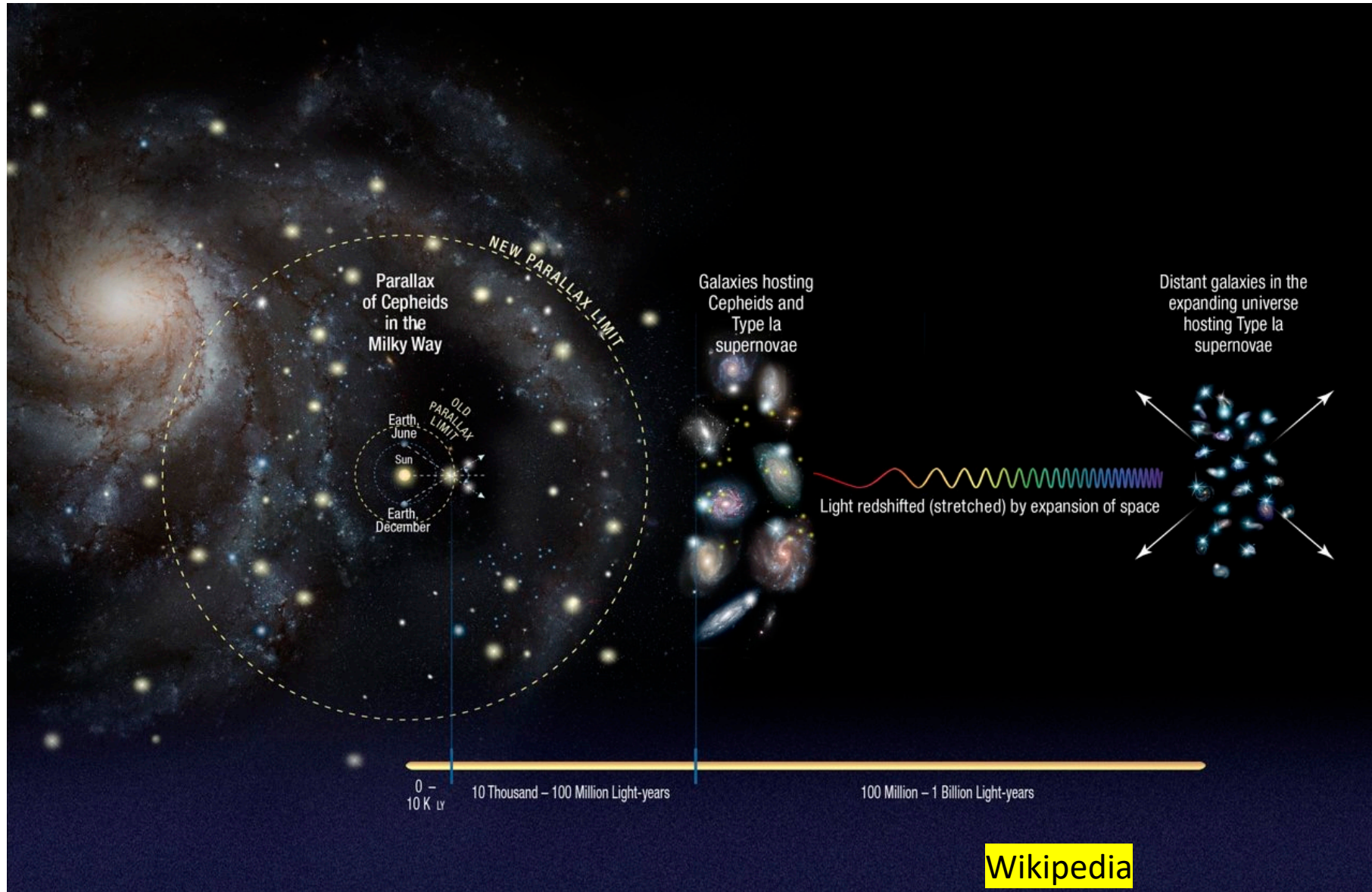


Cepheids → PL relations:  $M = a + b \log P$

”a” must be calibrated with geometric methods (e.g. parallaxes, detached eclipsing binaries)



# The «distance ladder» to measure $H_0$ : a three step process





# Cepheids and the cosmic distance ladder: a three step process (SH0ES project)

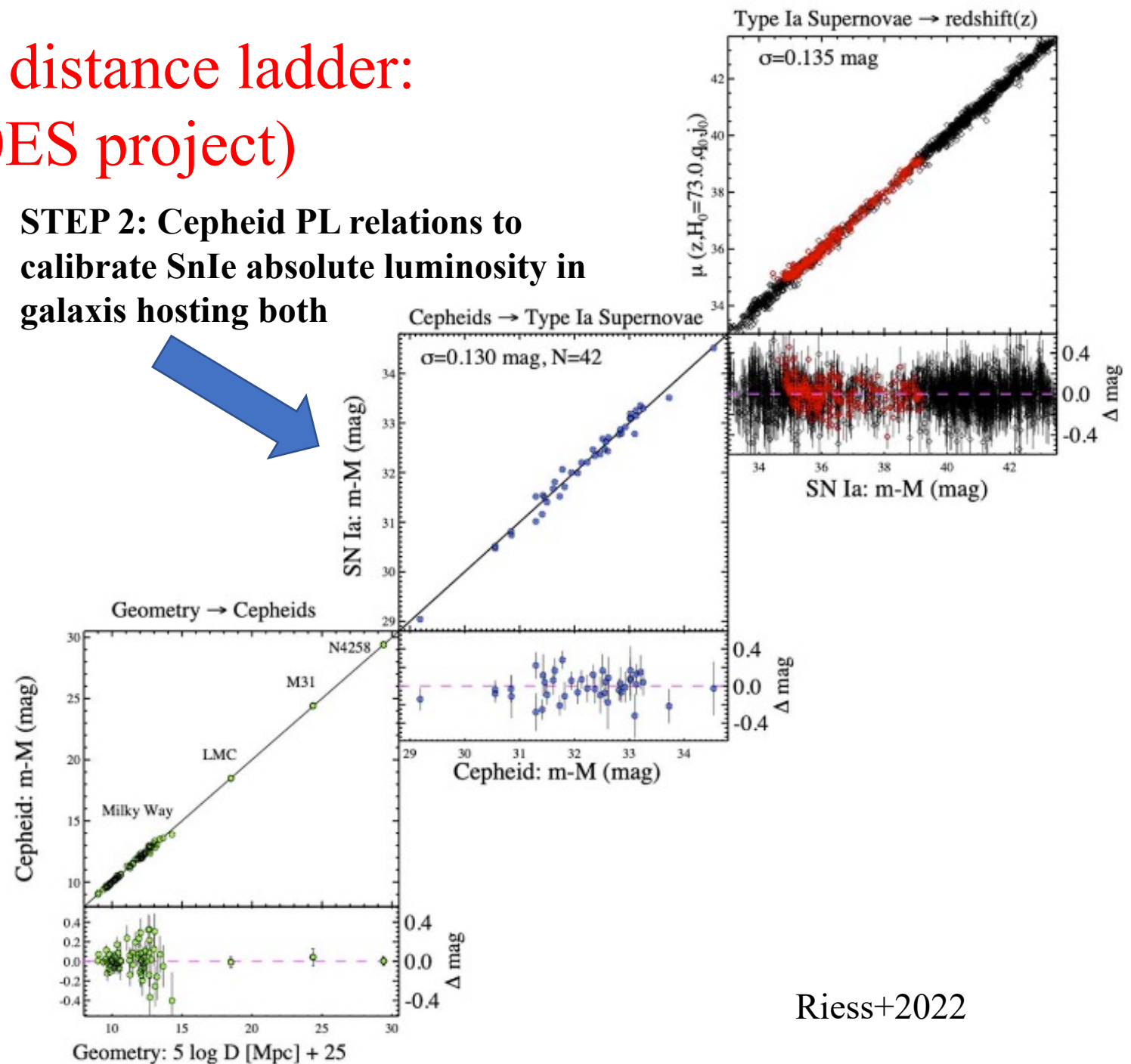
## STEP 1: Geometric distances to calibrate the PL relation of Cepheids:

- Parallaxes in the MW (HST, Gaia)
- Distance of LMC from DEBs
- Distance of NGC4258 from masers orbiting central supermassive black hole

Strong assumption:  
Universal PL relations

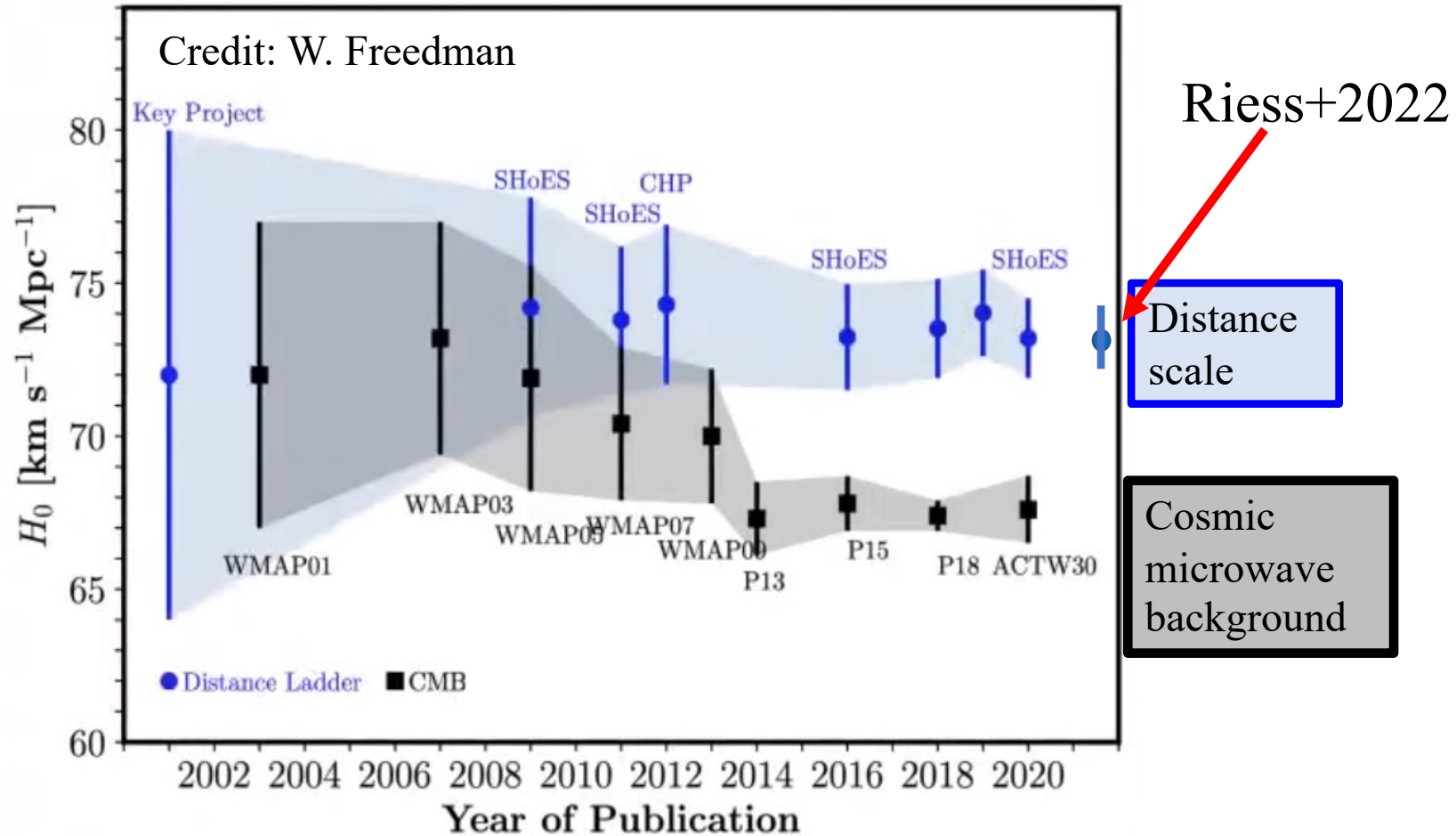
$$W_{\text{HST}} = F160W - 0.386 (F555W - F814W)$$

## STEP 2: Cepheid PL relations to calibrate SNIe absolute luminosity in galaxy hosting both



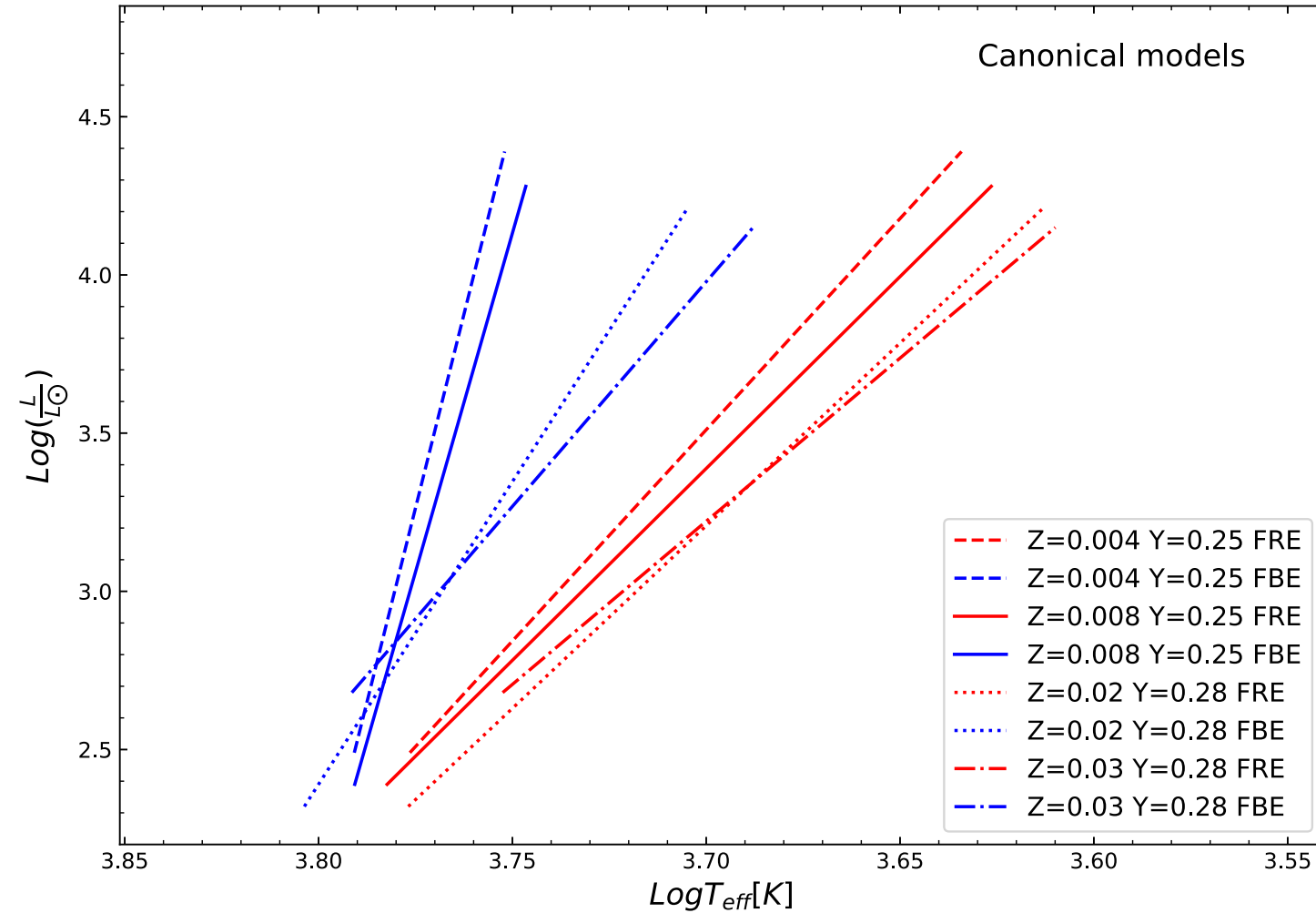
Riess+2022

# Hubble tension



All the sources of systematic errors in the cosmic distance scale must be analysed. One of these is the metallicity dependence of PL

# Period-Luminosity dependence on metallicity: Pulsation Theory

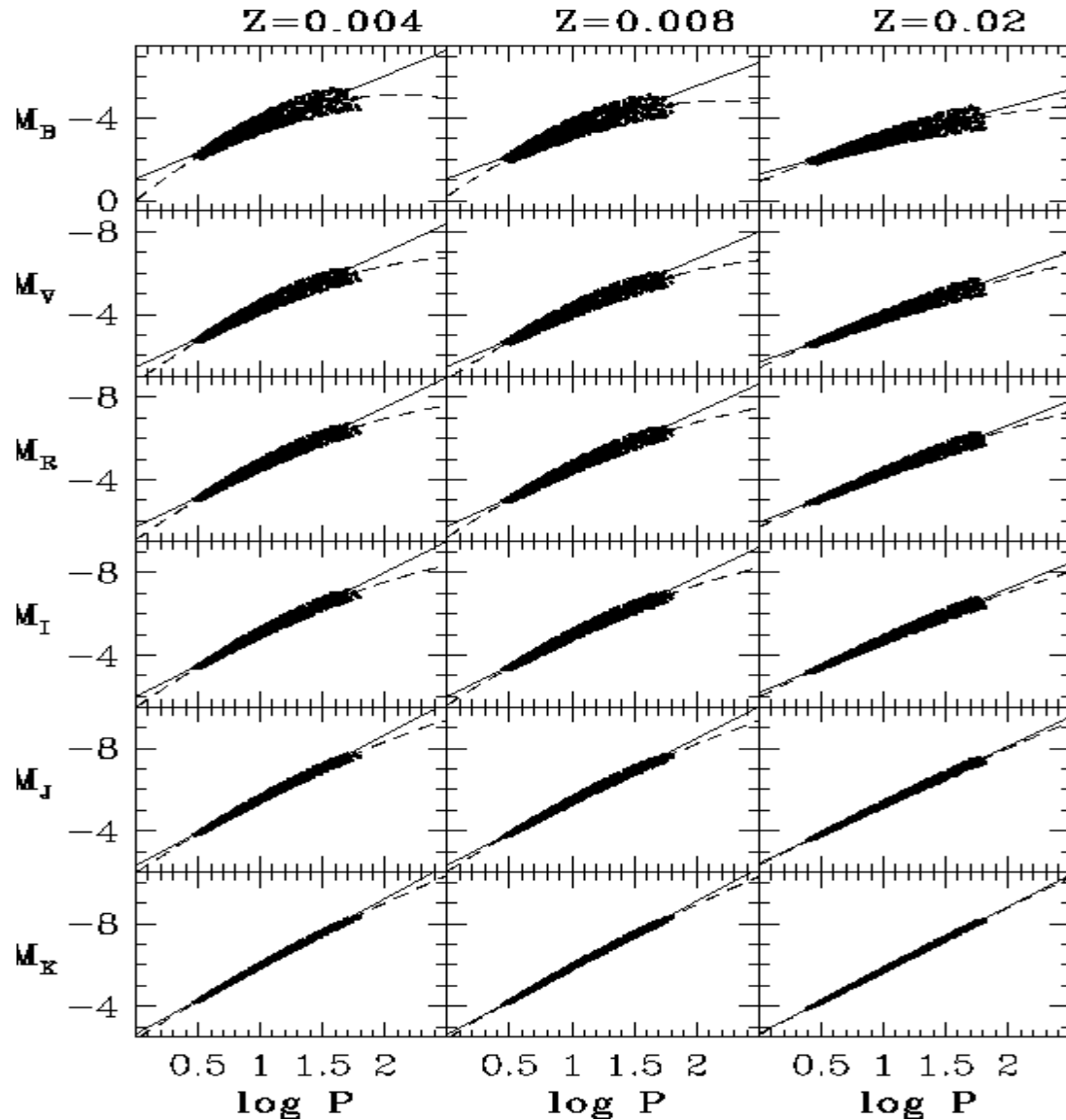


The Cepheids instability strip shifts towards cooler temperatures as the metallicity increases → impact on the PLRs

# Synthetic multiband PL relations

Optical

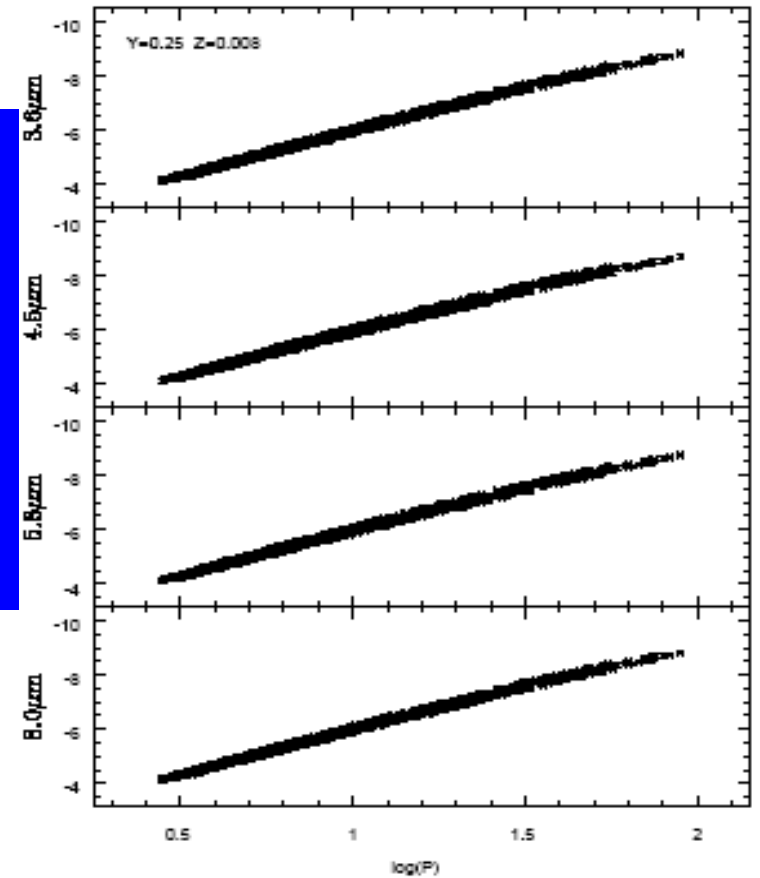
Near-Infrared



Synthetic multifilter PL relations

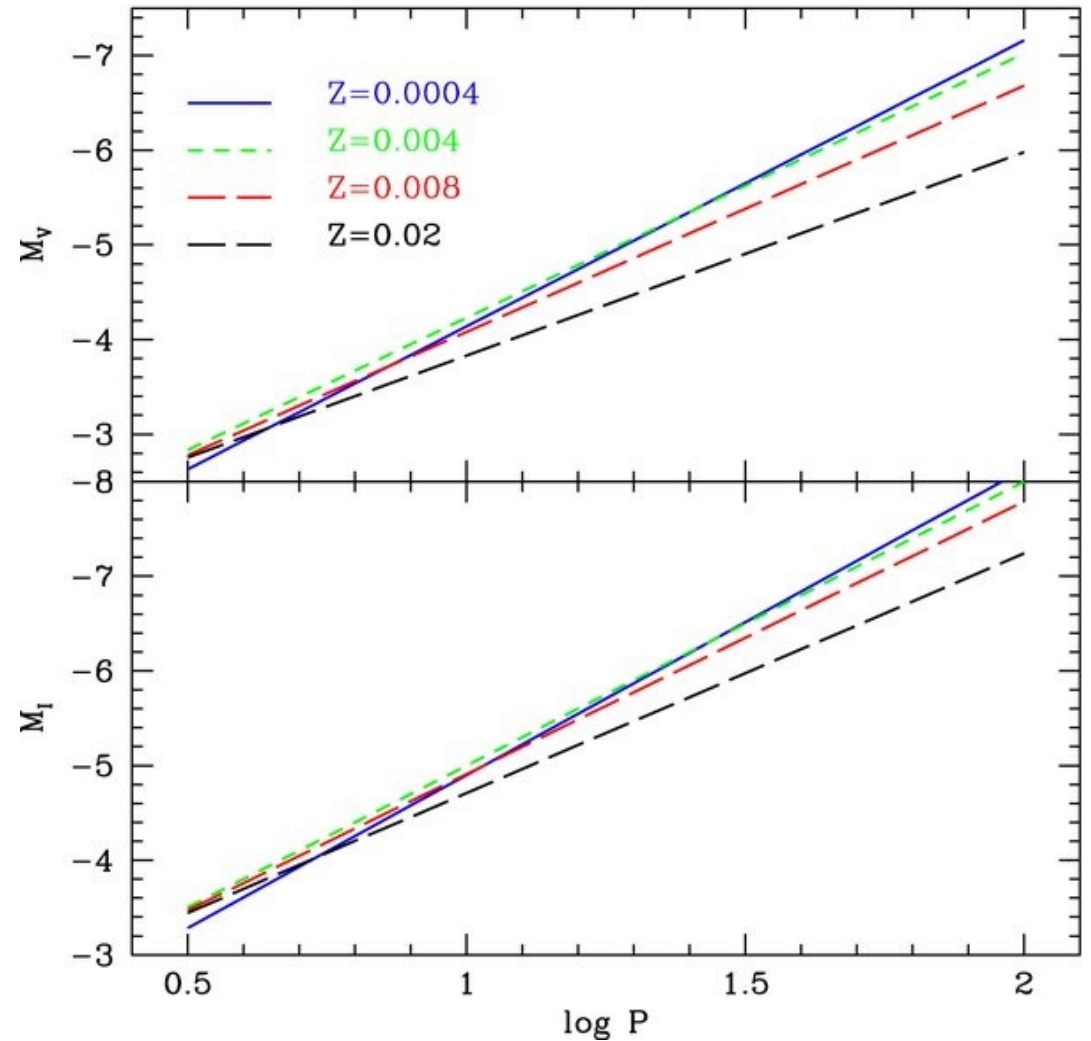
The effect reduces when moving towards longer wavelengths

Mid-Infrared



# Universal slope?

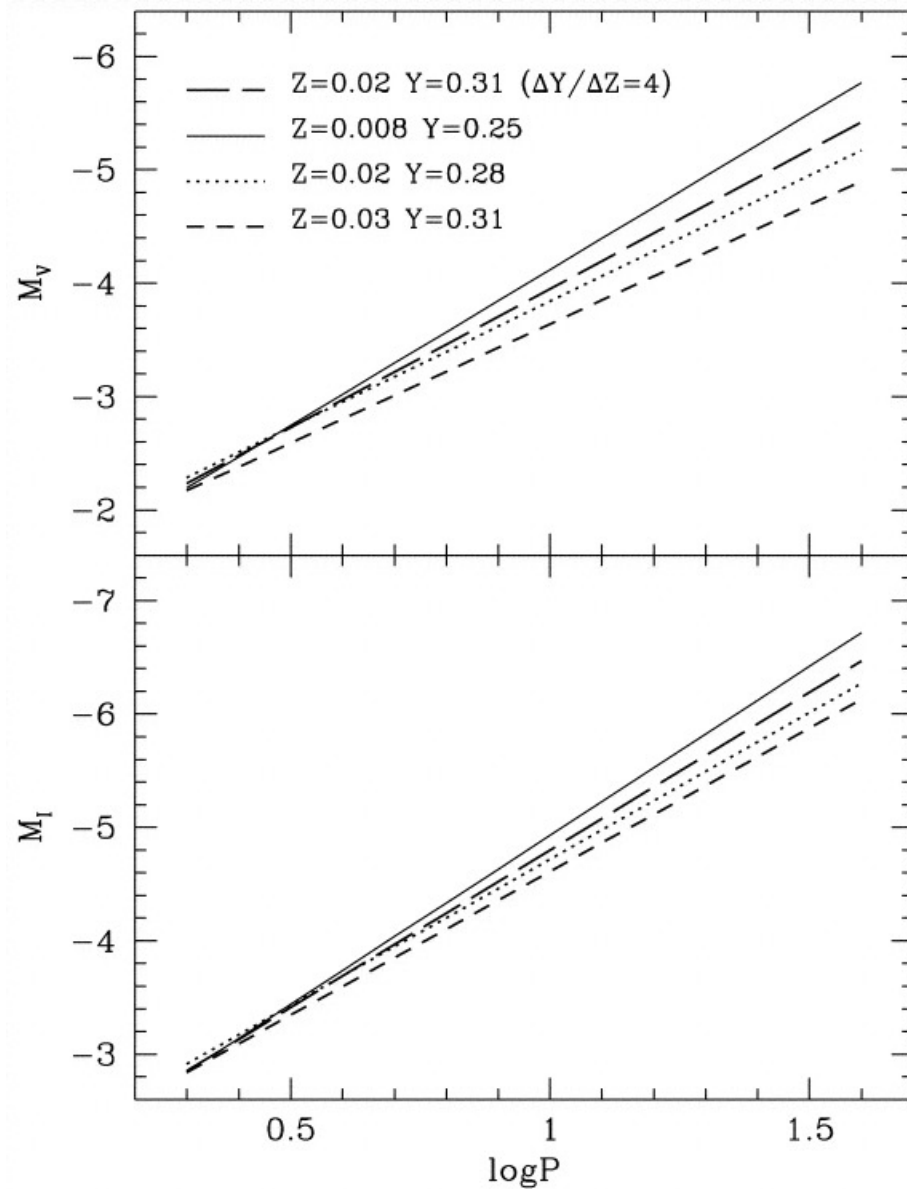
- The Cepheids' PL relation is often considered “Universal“, for example the same slope is used for all the galaxies
- However, models predict different slopes at different metallicities.
- Smaller effect at low metallicities
- Smaller effect at longer wavelenghts



*Marconi et al. 2010 ApJ (in agreement with results from the Araucaria project)*

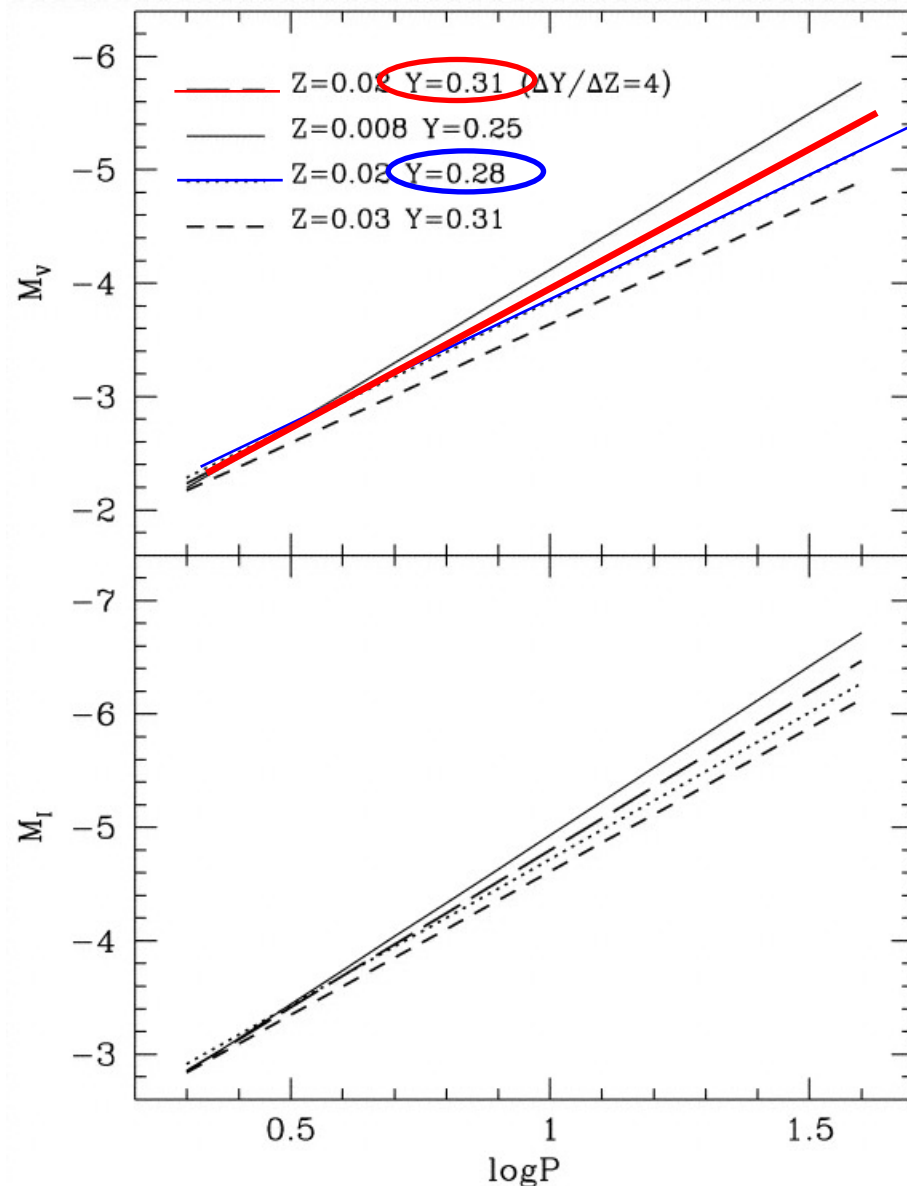


# Dependence of Cepheid properties on Helium abundance $\rightarrow \Delta Y / \Delta Z$



The slope **decreases** as **Z** increases at fixed  $\Delta Y / \Delta Z$

# Dependence of Cepheid properties on Helium abundance $\rightarrow \Delta Y / \Delta Z$



The slope **decreases** as **Z** increases at fixed  $\Delta Y/\Delta Z$

The slope **increases** as **Y** increases at fixed **Z**

As **Z** increases the PL gets flatter !!

As **Y** increases the PL gets steeper !!

## Parametrization of the metallicity dependence of PLRs

The most general formulation uses four parameters, to take into account the possible metallicity effect on the slope of PLRs, which is predicted by the models

$$M_{\lambda} = \alpha_{\lambda} + (\beta_{\lambda} + \delta_{\lambda}[\text{Fe}/\text{H}])\log P + \gamma_{\lambda}[\text{Fe}/\text{H}]$$

As this effect is mitigated at longer wavelength, usually  $\delta_{\lambda}$  is ignored.

$$M_{\lambda} = \alpha_{\lambda} + \beta_{\lambda}\log P + \gamma_{\lambda}[\text{Fe}/\text{H}]$$

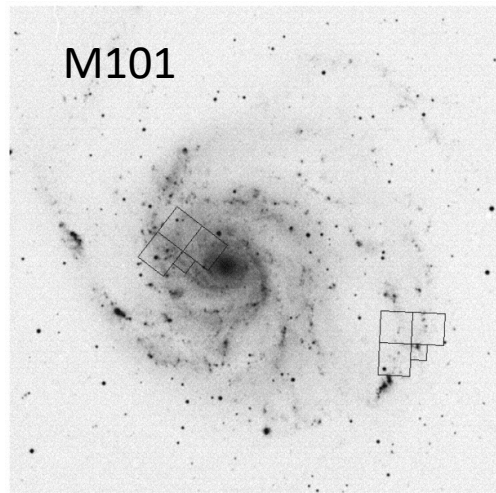
↑  
Intercept

↑  
Slope

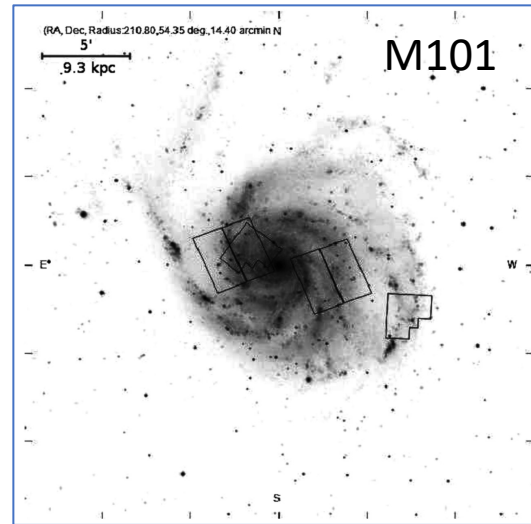
↑  
Metallicity  
term

# Empirical tests for metallicity effect

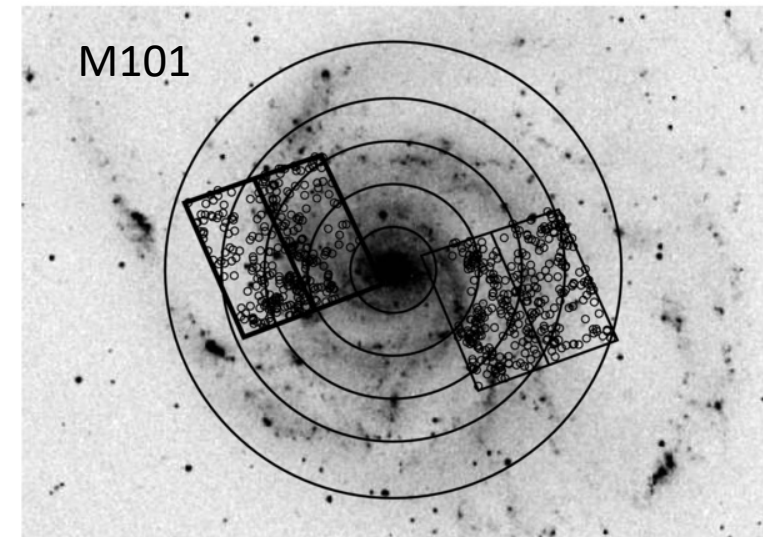
Several tests of the metallicity effect based on e.g.  
the comparison between Cepheids belonging to 2 fields with different metallicity in the same galaxy.  
The metallicity is estimated from the radial gradient of  $[O/H]$  measured in HII regions.



↓  
Kennicutt et al. 1998  
 $\Delta\mu/\Delta[O/H] = -0.24 \pm 0.16 \text{ mag dex}^{-1}$



Shappee & Stanek 2011:  
 $\Delta\mu/\Delta[O/H] = -0.76 \pm 0.3 \pm 0.2 \text{ mag dex}^{-1}$



Mager et al. 2013:  
 $\Delta\mu/\Delta[O/H] = -0.33 \text{ mag dex}^{-1}$

$$[O/H] \approx [Fe/H] + 0.09 \text{ dex (Romaniello+2022)}$$

# Metallicity dependence in the SHOES project

$$\mu_{0,i} = m_{i,H}^W - (M_{H,1}^W + b_W (\log P_i - 1) + Z_W \Delta[\text{O}/\text{H}]_i),$$

$$W_{\text{HST}} = F160W - 0.386 (F555W - F814W)$$

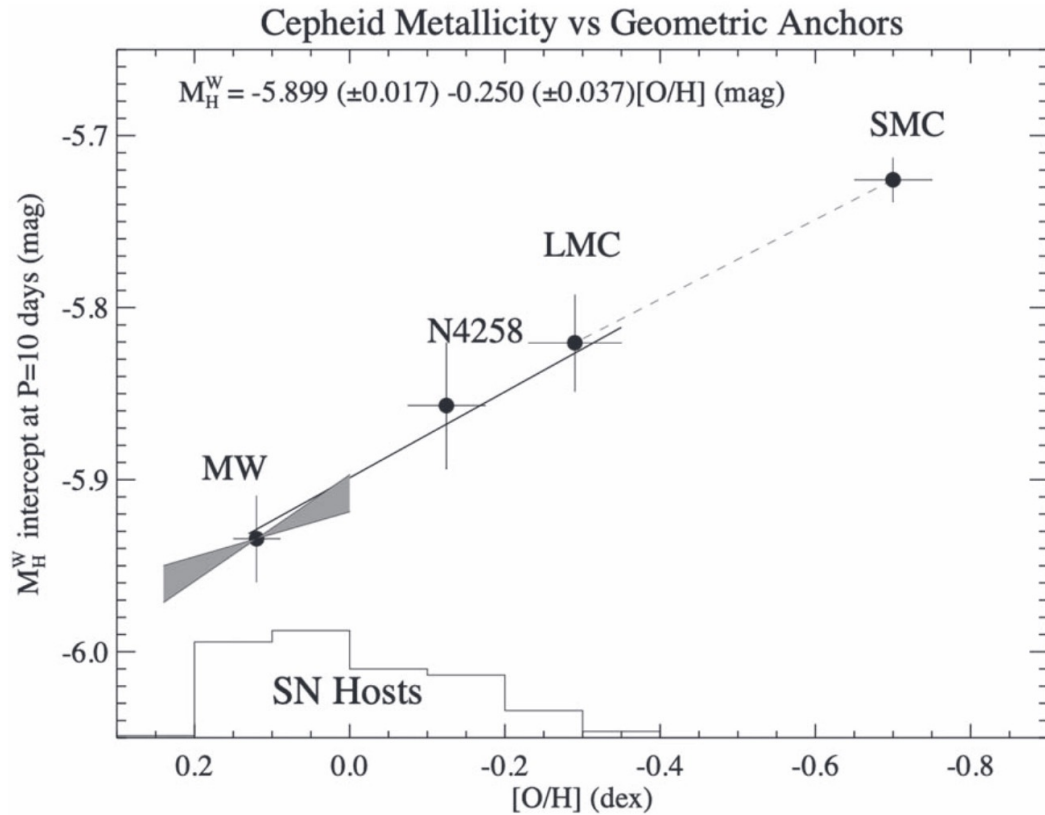
In the SHOES project the metallicity dependence is a result of the multi-parameter fit;  $\delta$  is neglected, the slope is the same for all the galaxies.

Their baseline value is

$$\gamma = -0.217 \pm 0.046 \text{ mag/dex}$$



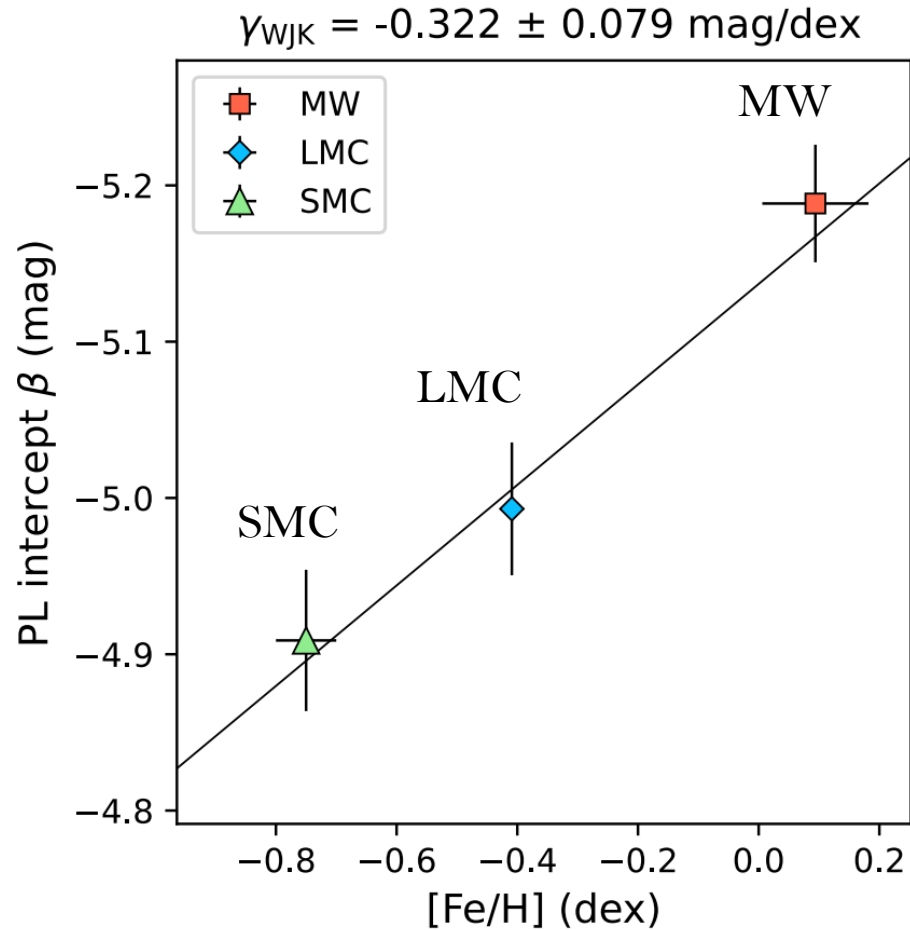
# Metallicity dependence in the SHOES project



According to the SHOES group, the metallicity problem should be mitigated by the fact that SNIa host galaxies have metallicities similar to those of the anchors.

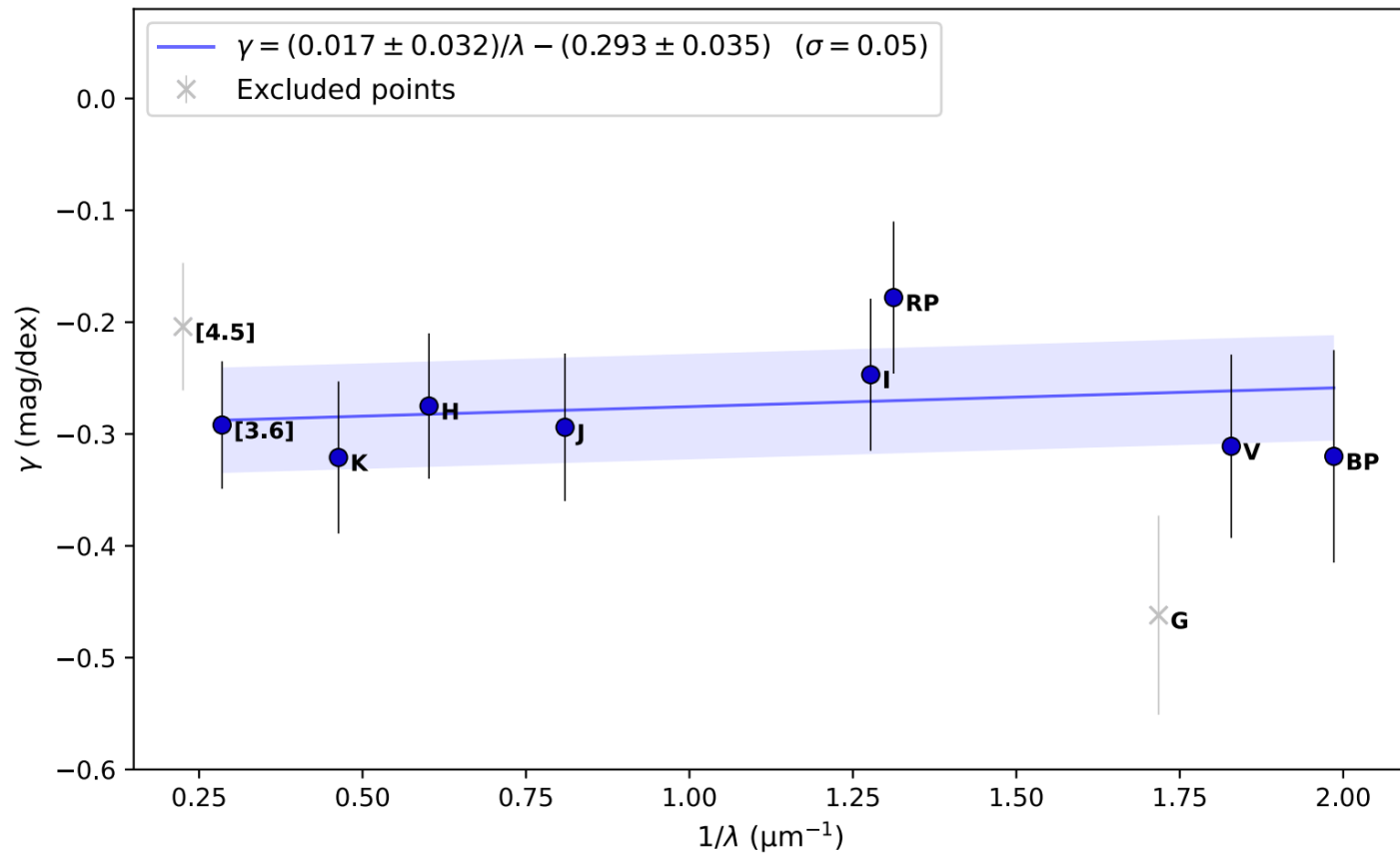
Yet, to reach the 1% precision on  $H_0$ , requires that we understand accurately the PLRs dependence on metallicity.

# Metallicity dependence using, MW, LMC, SMC



- Multiband PL relation with the same slope in the MW, LMC and SMC:  $\alpha^* + \beta \times \log P$
- The value of “ $\alpha^*$ ” is fixed:
  - with the Gaia parallaxes in the MW for a sample of  $\sim 180$  DCEPs close to the sun.
  - Geometric distances of LMC and SMC based on Detached Eclipsing Binaries (DEBs Pietrzyński+2019; Graczyk+2020)
- The MW is considered as “monometallic” ( $[Fe/H] = +0.08$  dex). LMC and SMC metallicities from High-Res spectroscopy.
- $\alpha^* = \alpha + \gamma \left[ \frac{Fe}{H} \right]$

# Metallicity dependence using, MW, LMC, SMC



$\gamma$  in the interval -0.2:-0.35 mag/dex

# Recent pulsation theory metallicity dependence estimates: Gaia Wesenheit $G-1.90(G_{BP}-G_{RP})$ and $W_{HST}$

PWZ Coefficients in the Gaia EDR3 Filters ( $W(G, G_{BP}-G_{RP}) = a + b(\log P - 1) + c[\text{Fe}/\text{H}]$ ) for F and FO CCs Derived by Adopting the A, B, and C ML Relations and  $\alpha_{ml} = 1.5, 1.7, \text{ and } 1.9$

| $\alpha_{ml}$ | ML | $a$    | $b$    | $c$    | $\sigma_a$ | $\sigma_b$ | $\sigma_c$ | $\sigma$ | $R^2$ |
|---------------|----|--------|--------|--------|------------|------------|------------|----------|-------|
| F             |    |        |        |        |            |            |            |          |       |
| 1.5           | A  | -6.018 | -3.314 | -0.189 | 0.009      | 0.016      | 0.021      | 0.118    | 0.993 |
| 1.7           | A  | -6.072 | -3.379 | -0.129 | 0.010      | 0.016      | 0.021      | 0.090    | 0.996 |
| 1.9           | A  | -6.170 | -3.472 | -0.245 | 0.023      | 0.018      | 0.040      | 0.072    | 0.998 |
| 1.5           | B  | -5.853 | -3.234 | -0.190 | 0.011      | 0.016      | 0.022      | 0.139    | 0.991 |
| 1.7           | B  | -5.871 | -3.262 | -0.260 | 0.012      | 0.015      | 0.023      | 0.118    | 0.995 |
| 1.9           | B  | -5.968 | -3.370 | -0.189 | 0.026      | 0.017      | 0.047      | 0.092    | 0.997 |
| 1.5           | C  | -5.694 | -3.270 | -0.105 | 0.012      | 0.017      | 0.023      | 0.141    | 0.991 |
| 1.7           | C  | -5.722 | -3.274 | -0.140 | 0.012      | 0.015      | 0.022      | 0.116    | 0.994 |
| 1.9           | C  | -5.800 | -3.327 | -0.167 | 0.023      | 0.016      | 0.043      | 0.094    | 0.997 |

**Table 20**

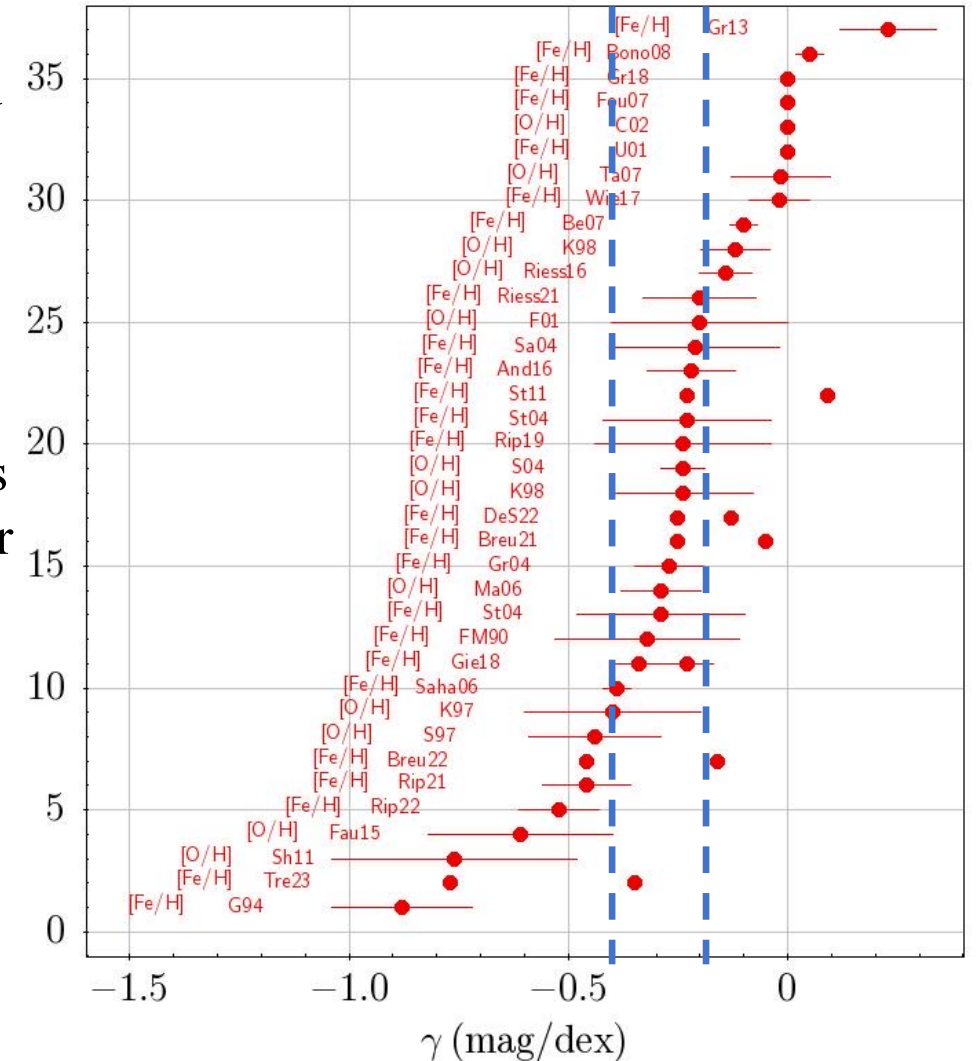
PWZ Coefficients in the HST-WFC3 Filters ( $W(F160W, F555W-F814W) = a + b(\log P - 1) + c[\text{Fe}/\text{H}]$ ) for F and FO CCs Derived by Adopting the A, B, and C ML Relations and  $\alpha_{ml} = 1.5, 1.7, \text{ and } 1.9$

| $\alpha_{ml}$ | ML | $a$    | $b$    | $c$    | $\sigma_a$ | $\sigma_b$ | $\sigma_c$ | $\sigma$ | $R^2$ |
|---------------|----|--------|--------|--------|------------|------------|------------|----------|-------|
| F             |    |        |        |        |            |            |            |          |       |
| 1.5           | A  | -6.023 | -3.340 | -0.161 | 0.008      | 0.015      | 0.019      | 0.109    | 0.994 |
| 1.7           | A  | -6.060 | -3.393 | -0.135 | 0.010      | 0.015      | 0.020      | 0.085    | 0.997 |
| 1.9           | A  | -6.155 | -3.484 | -0.195 | 0.022      | 0.017      | 0.038      | 0.067    | 0.998 |
| 1.5           | B  | -5.858 | -3.254 | -0.125 | 0.010      | 0.015      | 0.021      | 0.129    | 0.993 |
| 1.7           | B  | -5.865 | -3.280 | -0.121 | 0.011      | 0.014      | 0.021      | 0.110    | 0.995 |
| 1.9           | B  | -5.952 | -3.376 | -0.136 | 0.025      | 0.016      | 0.045      | 0.088    | 0.997 |
| 1.5           | C  | -5.702 | -3.274 | -0.145 | 0.011      | 0.016      | 0.021      | 0.127    | 0.993 |
| 1.7           | C  | -5.717 | -3.281 | -0.130 | 0.011      | 0.014      | 0.020      | 0.104    | 0.995 |
| 1.9           | C  | -5.782 | -3.329 | -0.110 | 0.022      | 0.015      | 0.040      | 0.088    | 0.997 |

The predicted value of  $\gamma_\lambda$  varies in the range  $-0.11 : -0.26$  mag/dex

# Metallicity dependence of PL

- Intercept of PL dependence on metallicity not well constrained empirically yet: most recent results:  
 $\gamma \sim -0.20$ :  $\sim -0.40$  mag/dex (e.g. Gieren+2018; Groenewegen+2018; Riess+2019,2021,2022; Ripepi+2019,2020,2021,2022; Breuval+2021,2022).
- The metallicity effect on both slope and zero point of the PLRs might not be critical for the estimate of  $H_0$ , but still relevant for measuring distances of individual galaxies:  
 $\Delta\gamma \sim 0.2$  (mag/dex) if  $\Delta[\text{Fe}/\text{H}] \sim \pm 0.2$  dex  $\rightarrow \Delta\mu \pm 0.04$  mag  
 $\rightarrow \Delta D \pm 2\%$
- Important to better constraint Cepheids models





# C-Metall

*Cepheids-Metallicity in the Leavitt Law*

<https://sites.google.com/inaf.it/c-metall/home>

# The C-MetaLL project

- Use Galactic Cepheids in conjunction with **Gaia parallaxes** to constrain the PLZ/PWZ relations but: i) **too narrow range in [Fe/H] in literature**; ii) **not enough stars with accurate NIR photometry, reddening estimates**.
  1. Significantly enlarge (+~300 objects) the sample of Cepheids with metallicity measured from high-resolution spectroscopy *HARPS-N@TNG; UVES@VLT; PEPSI@LBT; ESPADONS@CFHT* (~340 stars observed already; 90% complete).
  2. Enlarge the range of [Fe/H] adopted in the determination of the PLZ/PWZ relations up to values typical of the SMC or more metal poor.
  3. Obtain multiband g,r,i,z,J,H,Ks photometry for a large sample of Cepheids to obtain precise average magnitudes and individual reddening measurements (*30% complete*).



**MEASURE ACCURATE PLZ/PWZ RELATIONS BASED ON HOMOGENEOUS SPECTROSCOPY AND PHOTOMETRY**

# The Team

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Leibniz-Institute for Astrophysics Potsdam (DE)

Photometry, Spectroscopy  
Photometry  
Photometry  
Pulsational models  
Spectroscopy  
Pulsational models  
Photometry  
Pulsational models  
Spectroscopy  
Spectroscopy  
Photometry  
Spectroscopy

G. Catanzaro & E. Trentin (PhD)

*Abundance determination*



A. Bhardwaj  
*Photometry*



R. Molinaro  
*Data analysis*



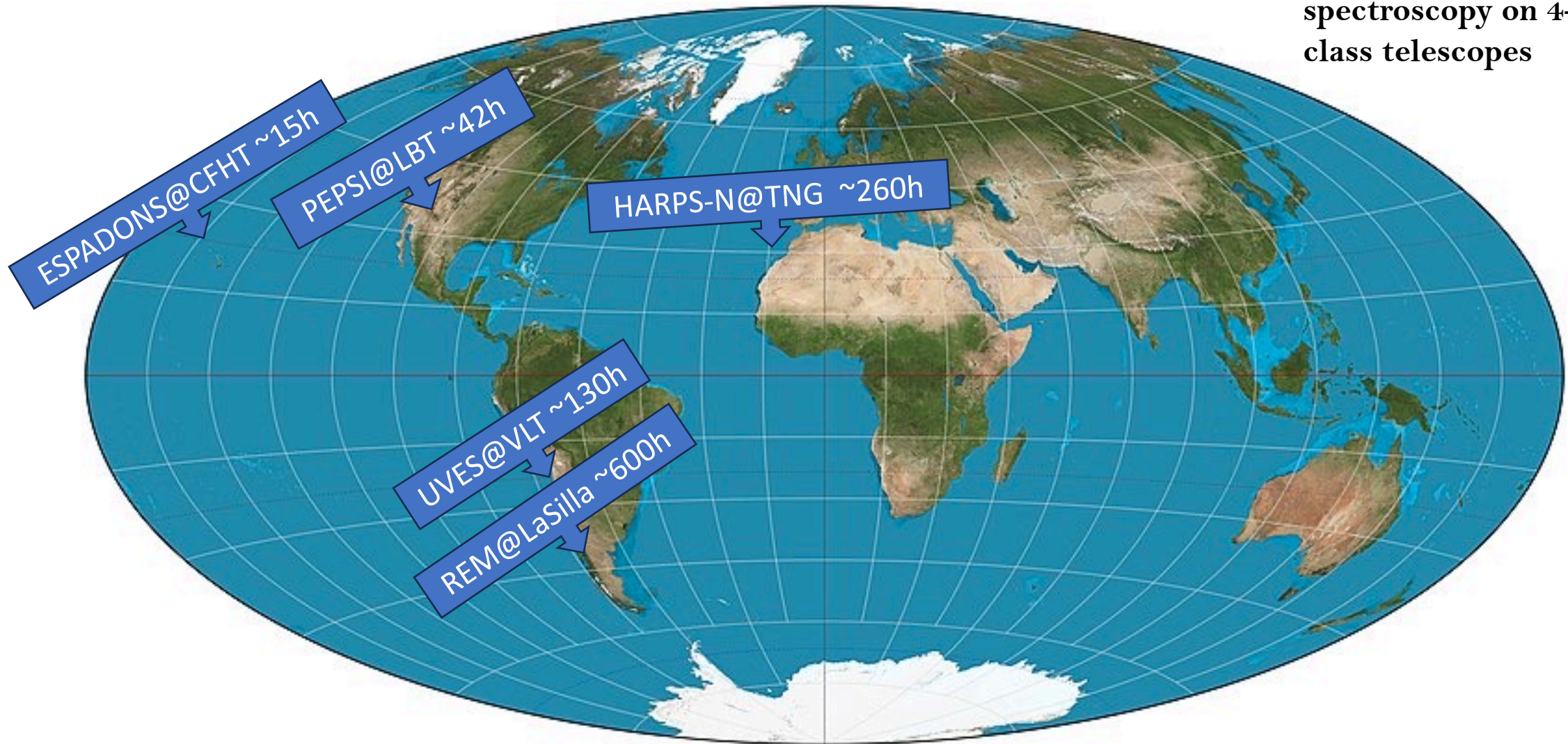
M. Marconi & G. De Somma  
*Pulsation theory*





# Observations

~450 h high-resolution spectroscopy on 4-8m class telescopes



# C-MetaLL Observations

| Instrument@<br>Telescope | n. DCEPs<br>Observed | n. DCEPs<br>Published | n. DCEPs<br>Next release |
|--------------------------|----------------------|-----------------------|--------------------------|
| HARPS-N@TNG              | 104                  | 49                    | 40                       |
| UVES@VLT                 | 166                  | 65                    | 101                      |
| PEPSI@LBT                | 22                   | 0                     | (22)                     |
| ESPADONS@CFHT            | 42                   | 0                     | 42                       |
| <b>Total</b>             | <b>340</b>           | <b>114</b>            | <b>180</b>               |

Spectroscopic observations started in 2019 and are still going on (TNG, VLT).

Next data release in preparation (Trentin et al. 2024, C-Metall VI).

|             | Bands    | n. DCEPs<br>Observed | n. DCEPs<br>Published |
|-------------|----------|----------------------|-----------------------|
| REM@LaSilla | grizJHKs | 88                   | 78                    |
| REM@LaSilla | grizH    | 92                   | 0                     |

REM restarted full operations in January 2021 (after pandemic)

Since January 2023 the REMIR filter-wheel is fixed on the H-band

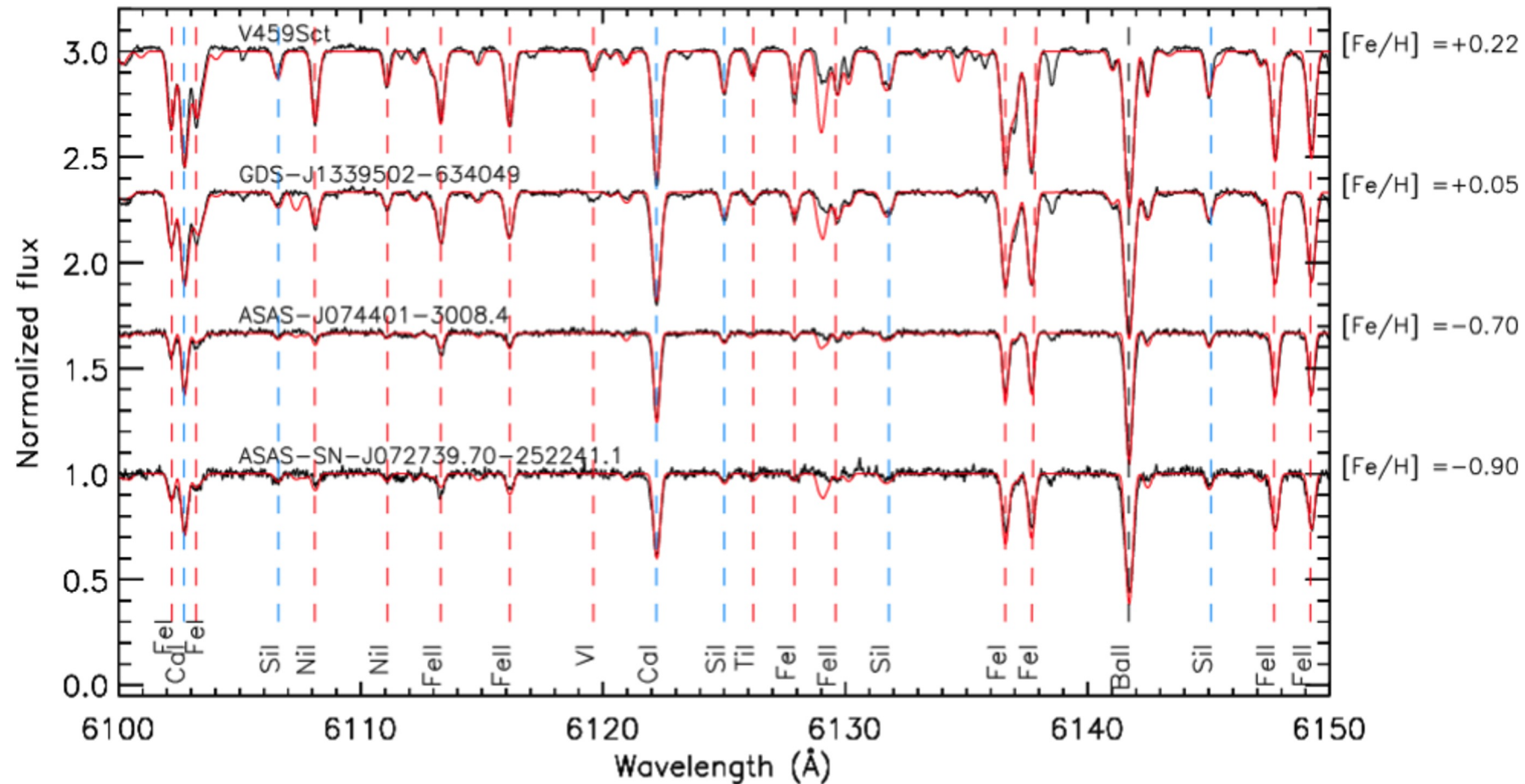
# C-MetaLL Early Results – Ripepi+2021(C-MetaLL-I), Ripepi+2022

- HARPS-N@TNG based abundances for 49 Galactic Cepheids
- Complementary literature spectroscopic and photometric data → sample ~490 Cepheids
- Using Gaia EDR3 parallaxes → PLZ/PWZ calibration in  $K_s$ ,  $W(J,K_s)$ ,  $W(V,K_s)$ ,  $W(H,V,I)$  (Ripepi+2021) and in  $W(G, G_{BP}, G_{RP})$  (Ripepi+2022)
- In Ripepi+2021 → i) larger metallicity dependence compared with Breuval+2021 and Riess+2021; ii) Counter-correction and metallicity term are anticorrelated.
- In Ripepi+2022 → PWZ in the Gaia bands: The metallicity dependence in the Gaia bands is even larger than in the other bands (Confirmed by Breuval+2022, Reyes&Anderson 2023)



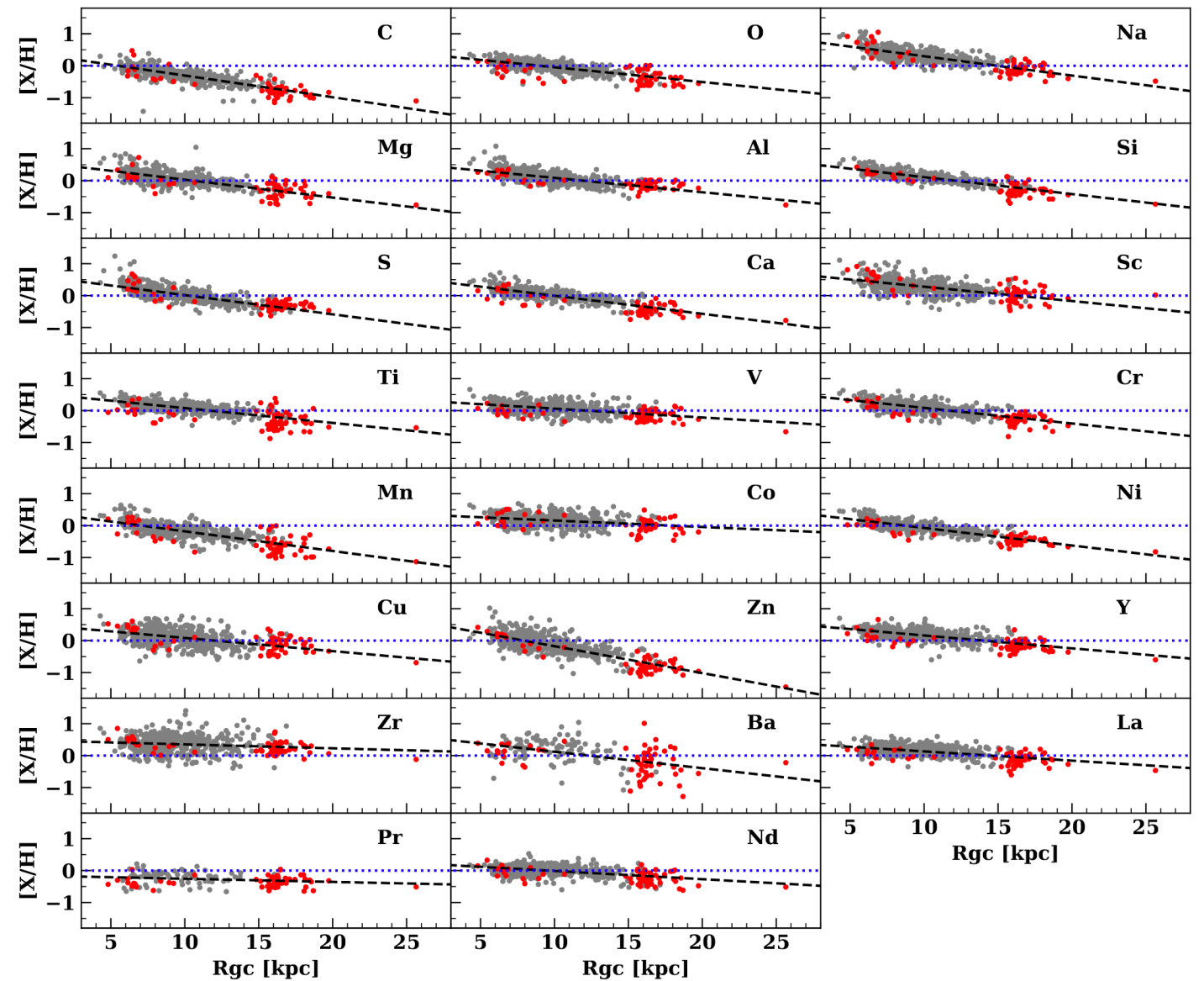
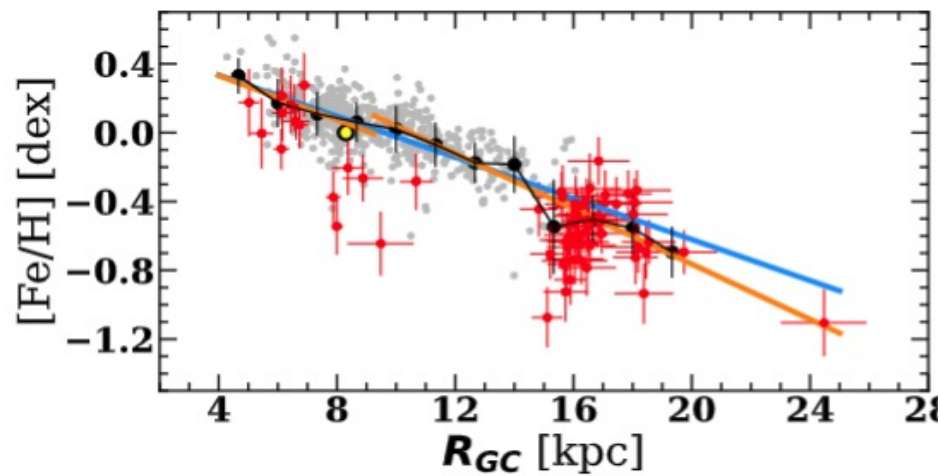
# C-MetaLL Results – Trentin et al. 2023 (C-MetaLL-II)

- UVES@VLT HiRes spectroscopy for additional 65 Cepheids
- $\sim 50$  faint objects chosen in the anticenter direction to have low metallicity.



# C-Metal Results – Trentin et al. 2023 (C-MetaLL II)

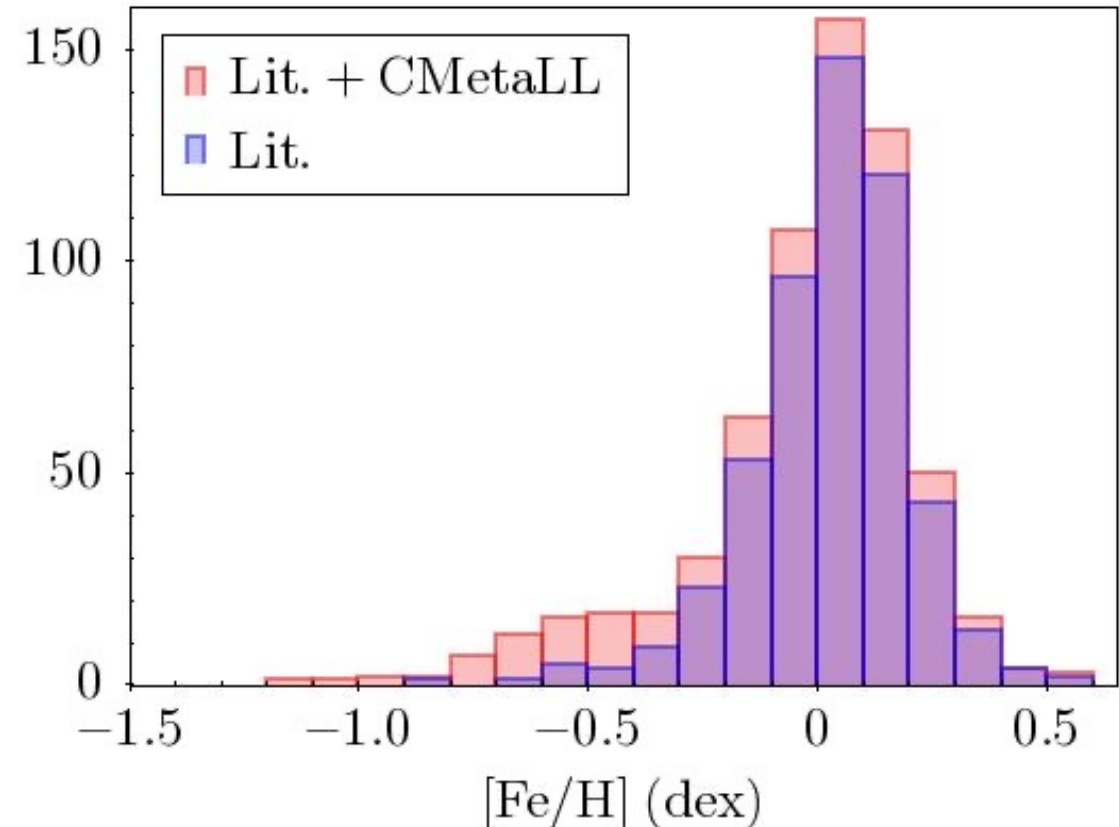
- Study of the metallicity gradient of the MW disc for 23 elements
- Possible break at 9.25 kpc



# Current baseline results of the C-MetaLL project

# C-MetaLL results: New calibration of multi-band PLZ/PWZ relations Trentin et al. 2024 (C-MetaLL IV)

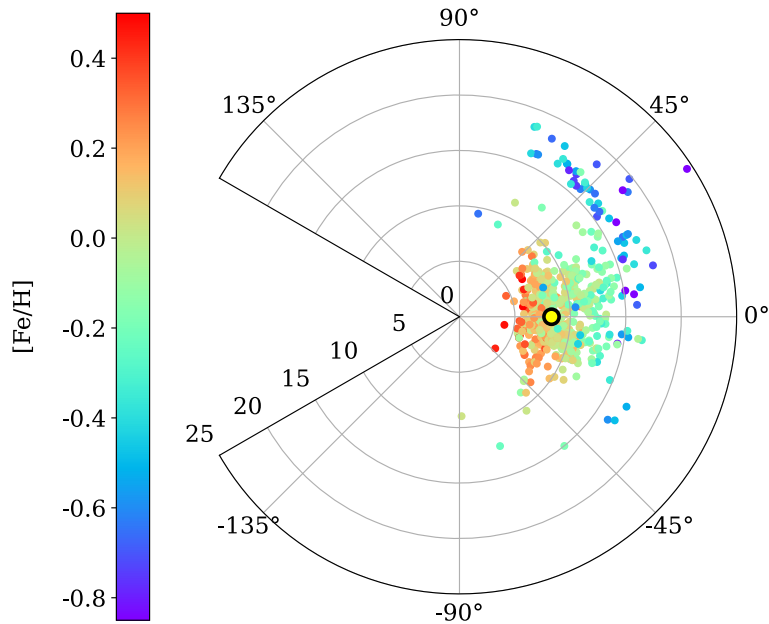
- Improved Cepheid sample thanks to C-MetaLL data (114 stars in total) and additional HiRes abundances for 68 Cepheids by Kovtyukh+2022
- Sample HiRes = 635 objects
- Plus 275 Cepheids with Gaia RVS  $[M/H]$  estimates (with good flags)  $\rightarrow$  total 910 Classical Cepheids (all data published in the paper).
- Optical G,  $G_{BP}$ ,  $G_{RP}$ , V, I and NIR photometry from the literature (more than 50% JHKs photometry from 1-epoch 2MASS data).
- Reddening from the literature or calculated (PC relations)



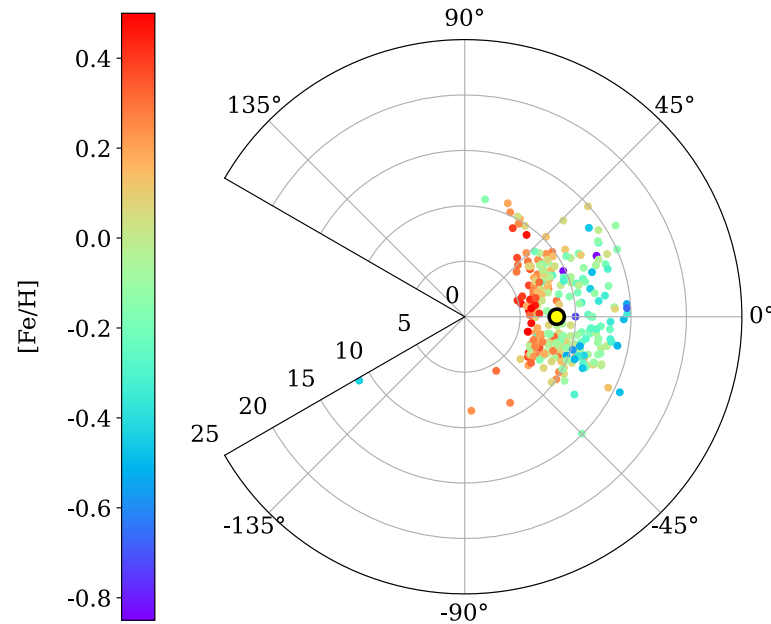
# Trentin et al. 2024 (C-MetaLL-IV): The sample

- HighRes data including Groenewegen2018, Ripepi+2021, Kovtyukh+2022, Trentin+2023
- Gaia RVS abundances (Recio-Blanco+2023)

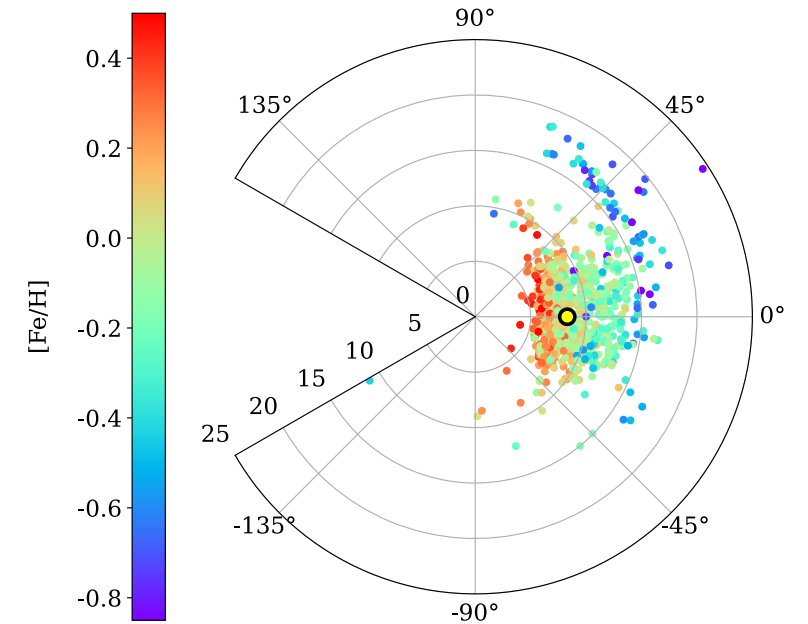
635 HiRes



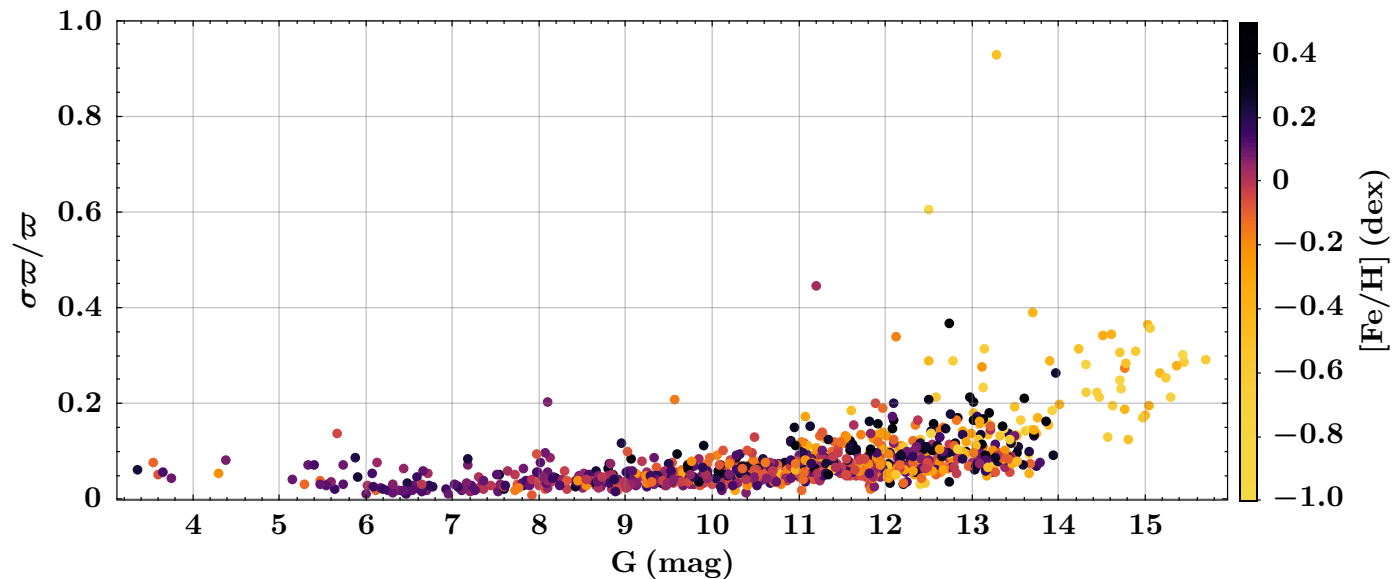
275 Gaia RVS



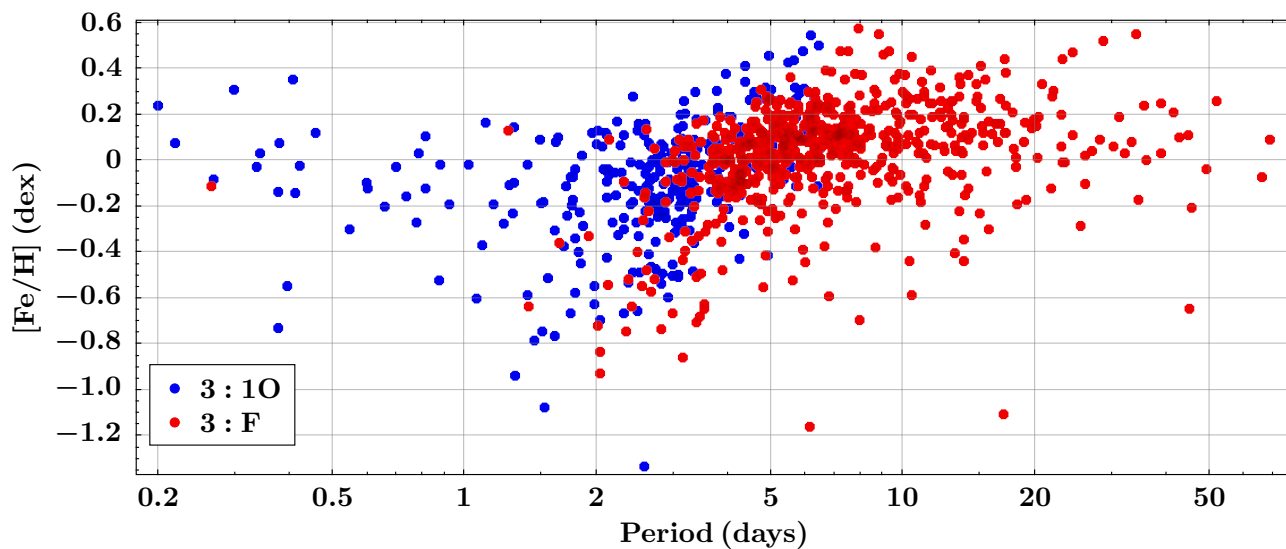
910 Total



# Properties of the sample



- Metal-poor objects are more distant in the anticentre direction  
→ generally less precise parallaxes → observe more metal-poor Cepheids to compensate lower precision with increased statistics.

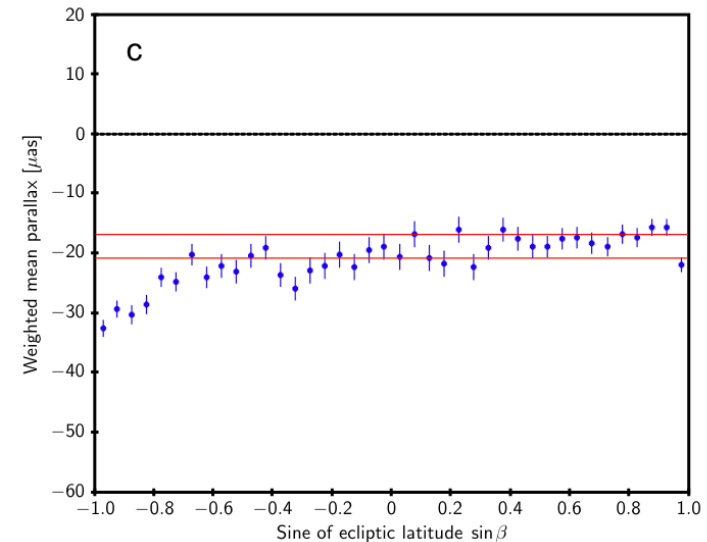
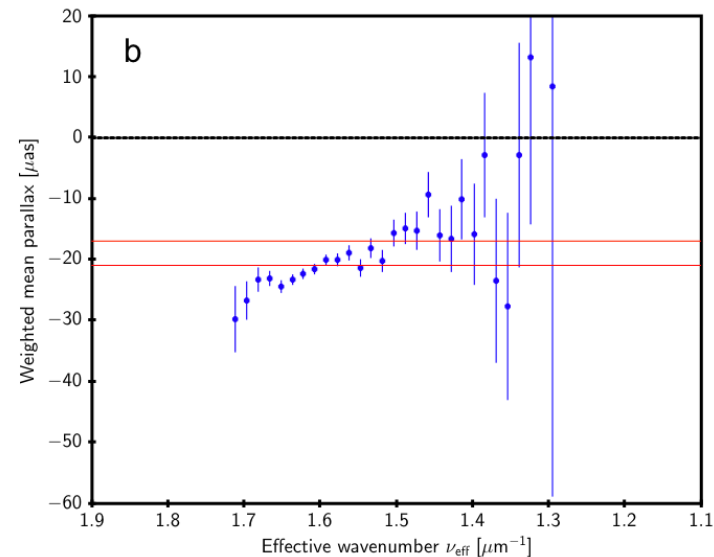
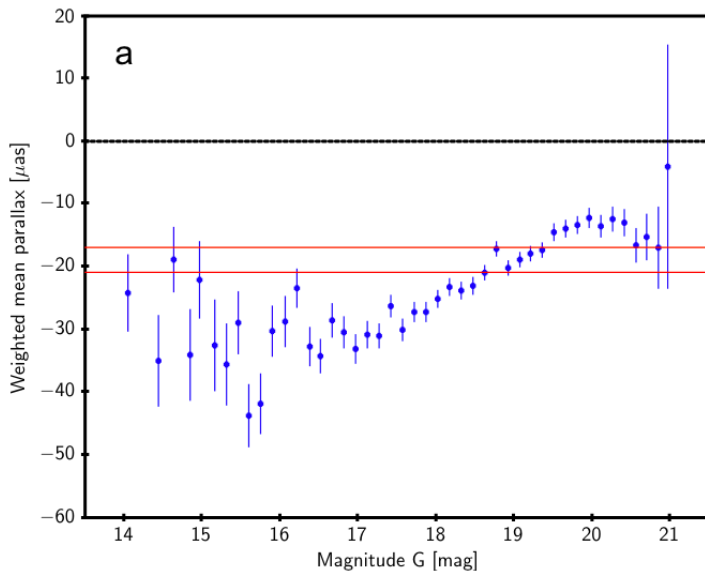


- There are few metal-poor objects with periods  $> 15$  days  
→ observe specifically those objects to fill the parameter space



# Gaia Parallax zero point offset (PZPO)

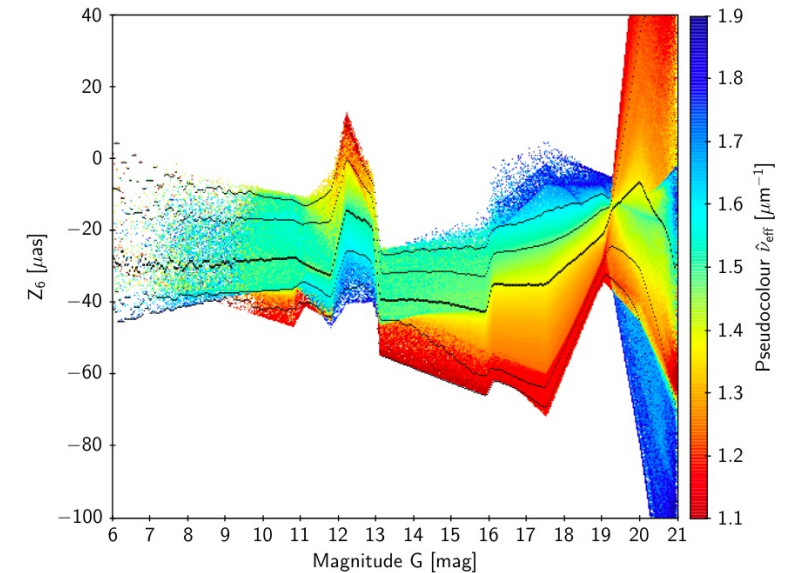
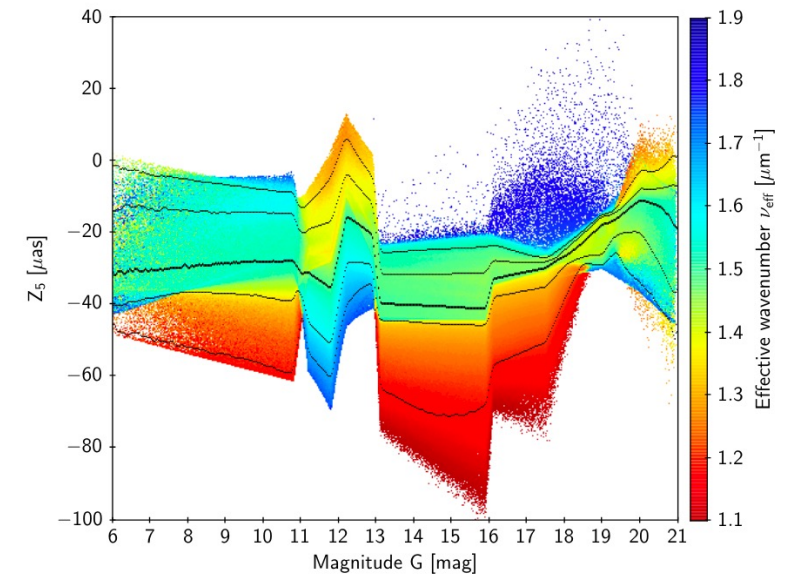
- Distribution of measured QSO parallaxes: average should be around zero: It is not
- Certain perturbations of the basic angle are observationally indistinguishable from a global shift of the parallaxes (Butkevich+2017)
- Average effect for QSO on average  $\sim 29 \mu\text{as}$  in DR2 and  $19 \mu\text{as}$  in DR3 (Arenou+2018, Lindegren+2021)



# Gaia Parallax zero point offset (PZPO)

$$\varpi_{\text{True}} = \varpi_{\text{Gaia}} - \text{PZPO}$$

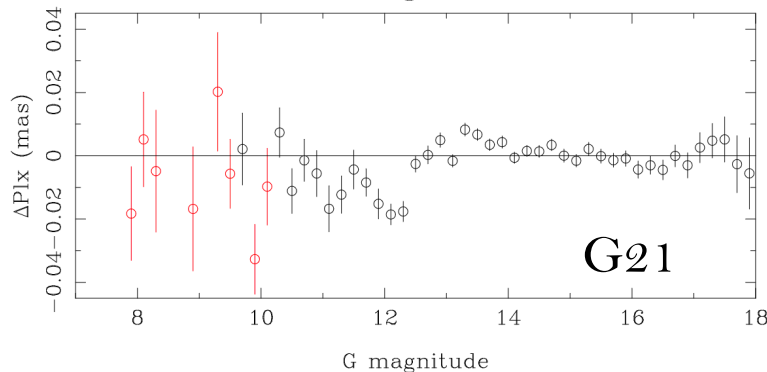
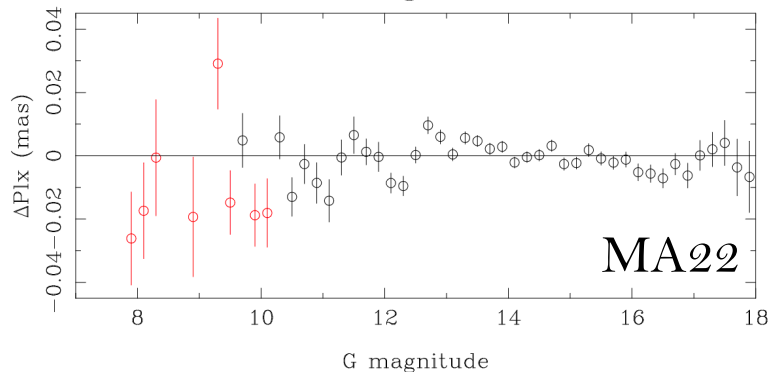
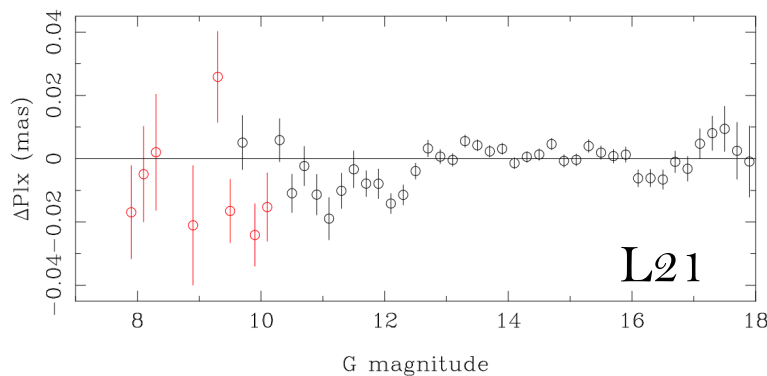
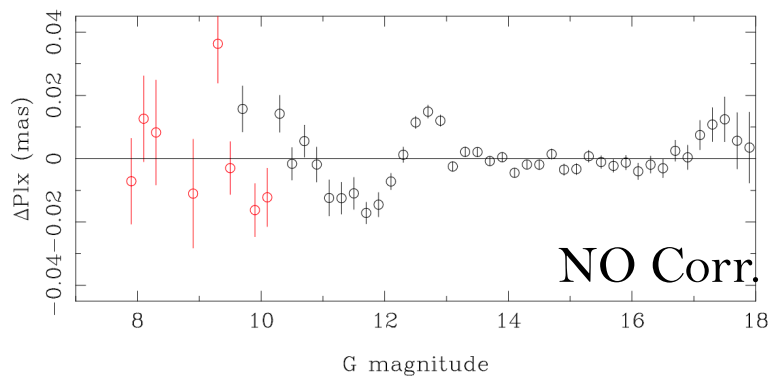
- The PZPO depends on Magnitude, colour, ecliptic latitude
- Lindegren+2021 (L21) provided individual offsets based on parallax comparison with QSO, Binaries and LMC
- Other corrections in the literature: Maíz Apellániz 2022 (MA22), Groenewegen 2021 (G21)



Lindegren+2021

# Gaia Parallax zero point offset (PZPO)

$$\varpi_{\text{True}} = \varpi_{\text{Gaia}} - \text{PZPO}$$

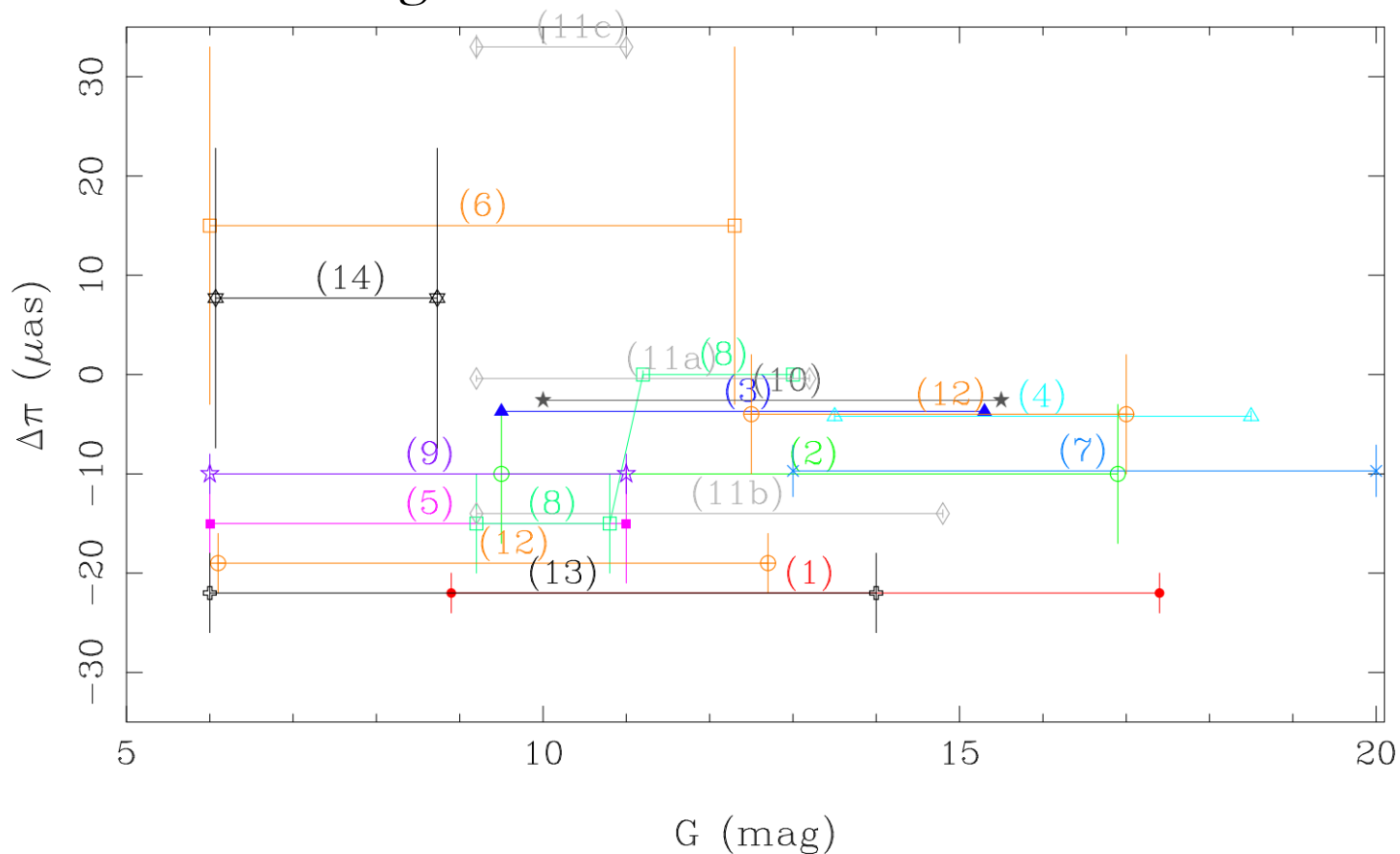


Test of the correction using open clusters.

Residuals between individual and cluster parallaxes summed over all clusters and plotted against G magnitude.  $\rightarrow$  no correction is perfect

| <i>G</i><br>(mag)       | no PZPO<br>( $\mu\text{as}$ ) | L21<br>( $\mu\text{as}$ ) | MA22<br>( $\mu\text{as}$ ) | G21<br>( $\mu\text{as}$ ) |
|-------------------------|-------------------------------|---------------------------|----------------------------|---------------------------|
| All                     | 9.78                          | 9.37                      | 9.45                       | 9.41                      |
| $G \leq 13$ mag         | 13.37                         | 12.83                     | 13.10                      | 13.06                     |
| $13 < G < 17$ mag       | 2.35                          | 3.48                      | 3.60                       | 3.39                      |
| $17 \leq G \leq 18$ mag | 8.62                          | 6.06                      | 3.97                       | 4.33                      |

## Groenewegen 2023



**Figure 3.** Counter-correction  $\Delta\pi$  plotted against magnitude for (1) Bhardwaj et al. (2021), RRL; (2) Gilligan et al. (2021), RRL; (3) Huang et al. (2021b), red clump (5p solution); (4) Ren et al. (2021), WUMa EBs (5p solution); (5) Riess et al. (2021a), DCEP LMC; (6) Stassun and Torres (2021), EBs; (7) Vasiliev and Baumgardt (2021), globular clusters; (8) Zinn (2021), asteroseismology; (9) Flynn et al. (2022), open/globular clusters;  $Bp - Rp > 1$  (10) Wang et al. (2022), giants; (11) Khan et al. (2023) red giants: asteroseismology, for the (a) *Kepler*, (b) *K2*, and (c) *TESS*-SCVZ fields ('E20', APOGEE DR17 values); (12) Cruz Reyes and Anderson (2023) Clusters ( $G = 12.5 - 17$  mag,  $0.8 < Bp - Rp < 2.75$  mag) and MW DCEPs; (13) Molinaro et al. (2023) MW DCEPs; (14) Groenewegen (2023) dynamical parallax of binary systems with spectroscopic and astrometric orbits.

## PZPO counter-correction

$$\varpi_{\text{True}} = \varpi_{\text{Gaia}} - \text{PZPO} + \Delta\varpi$$

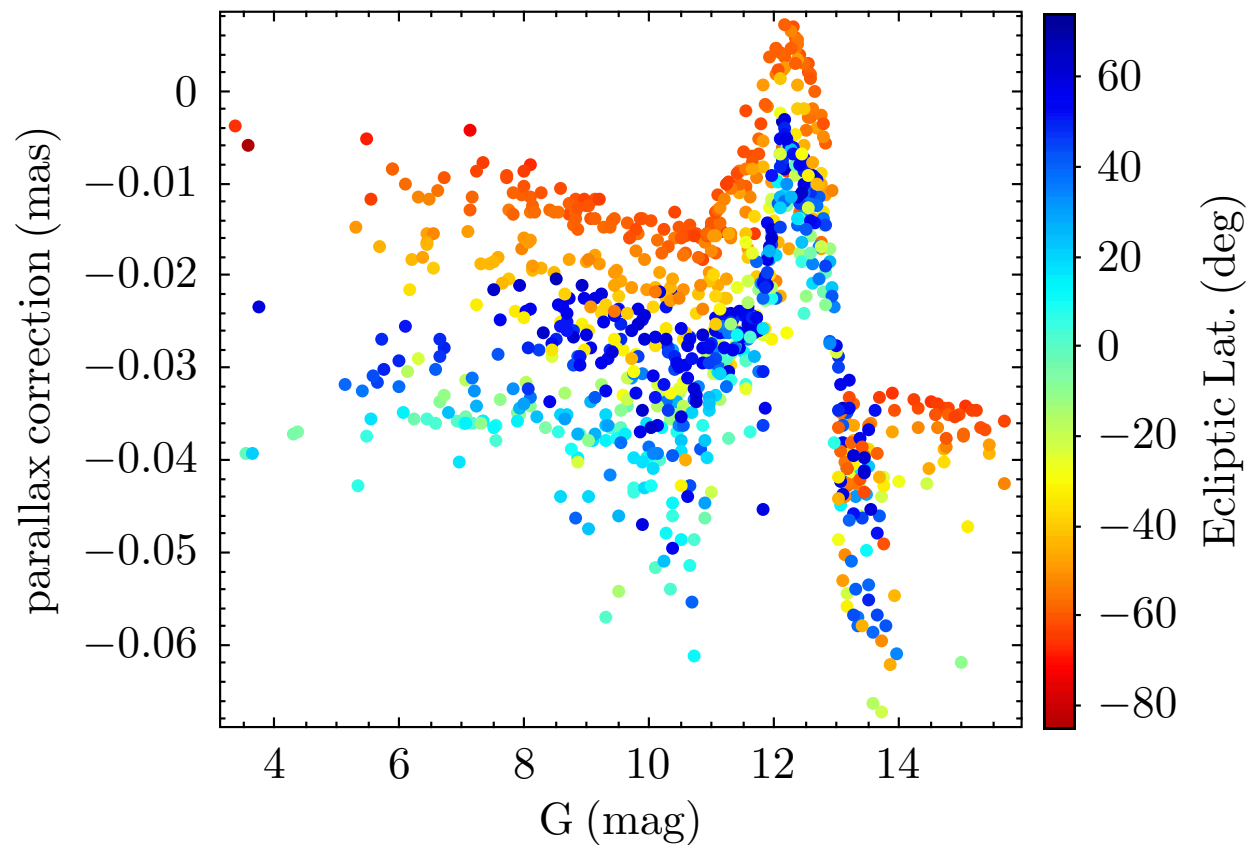
$\Delta\varpi$  is usually negative

No consensus on its value/error

The size of this counter-correction and the precision of its estimate may have a significant impact on the extra-galactic distance scale.

$\Delta\varpi = \pm 4 \mu\text{as} \rightarrow \pm 0.02$  mag at the distance of the LMC  $\rightarrow$  1% in distance  $\rightarrow$  1% on  $H_0$

# Preparation of the sample



- Gaia EDR3 parallaxes PZPO corrected with Lindegren+2021 recipe.
- Complex dependence on Magnitude, colour and ecliptic latitude.
- Used RUWE (Lindegren+2018) and fidelity\_v2 (Rybizki+2022) to cut-off objects with bad astrometry.

# ABL fitting

To avoid bias problems, the **Astrometry-Based Luminosity (ABL)** method (Arenou & Luri 1999; Gaia Collaboration+2017): **linear in parallax; no selection on parallax (negative parallaxes are included) nor on  $\sigma\pi/\pi$  is needed.**

$$ABL = 10^{0.2M_\lambda} = \pi 10^{(0.2m_{\lambda_0} - 0.2)}$$

$$M_\lambda = \alpha_\lambda + (\beta_\lambda + \delta_\lambda[\text{Fe}/\text{H}])\log P + \gamma_\lambda[\text{Fe}/\text{H}]$$

$$ABL = \varpi 10^{0.2m-2} = 10^{0.2(\alpha + (\beta + \delta[\text{Fe}/\text{H}])(\log P - \log P_0) + \gamma[\text{Fe}/\text{H}])},$$

The diagram illustrates the classification of terms in the ABL equation. The word "Observed" is positioned below the first part of the equation, and "Unknowns" is positioned below the second part. Blue arrows point from the terms in the equation to these labels:  $\varpi$  and  $10^{0.2m-2}$  are linked to "Observed";  $\alpha$ ,  $\beta$ ,  $\delta$ ,  $\gamma$ , and  $\log P - \log P_0$  are linked to "Unknowns".

Non-linear fitting, robust errors with bootstrap procedure



# ABL fitting

- We consider PL relations in G,  $G_{BP}$ ,  $G_{RP}$ , V, I, J, H, K<sub>S</sub>
- Cardelli+1989 reddening law to deal with extinction

Wesenheit magnitudes considered in this work

| Bands                   | $\lambda$ |
|-------------------------|-----------|
| $W_{G,G_{BP}-G_{RP}}$   | 1.9       |
| $W_{H,V-I}$             | 0.461     |
| $W_{F160W,F555W-F814W}$ | 0.386     |
| $W_{K_S,V-K_S}$         | 0.130     |
| $W_{K_S,J-K_S}$         | 0.690     |

# Data analysis

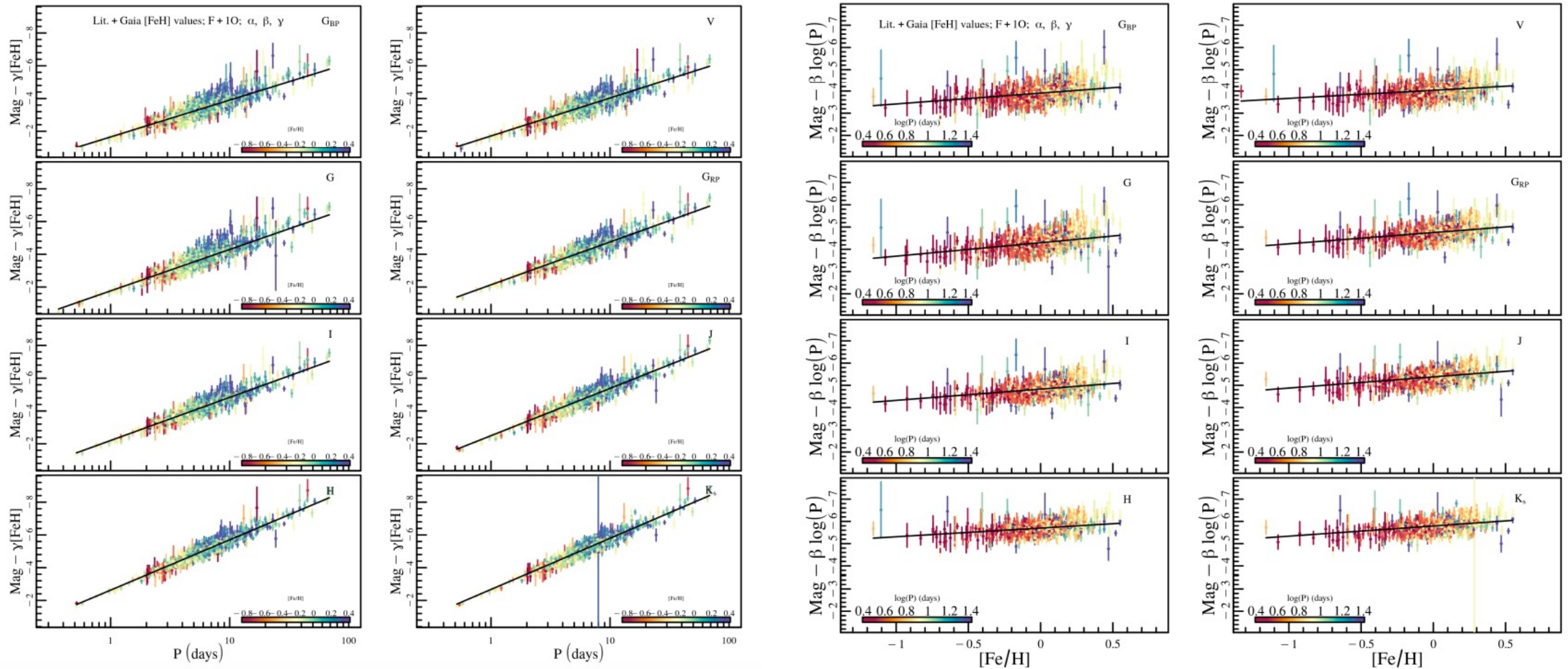
Several possibilities were explored:

1. With and without Gaia RVS abundances
2. With and without fundamentalised 1O pulsators
3. With different fixed counter-correction from the literature
4. With binning the data in metallicity

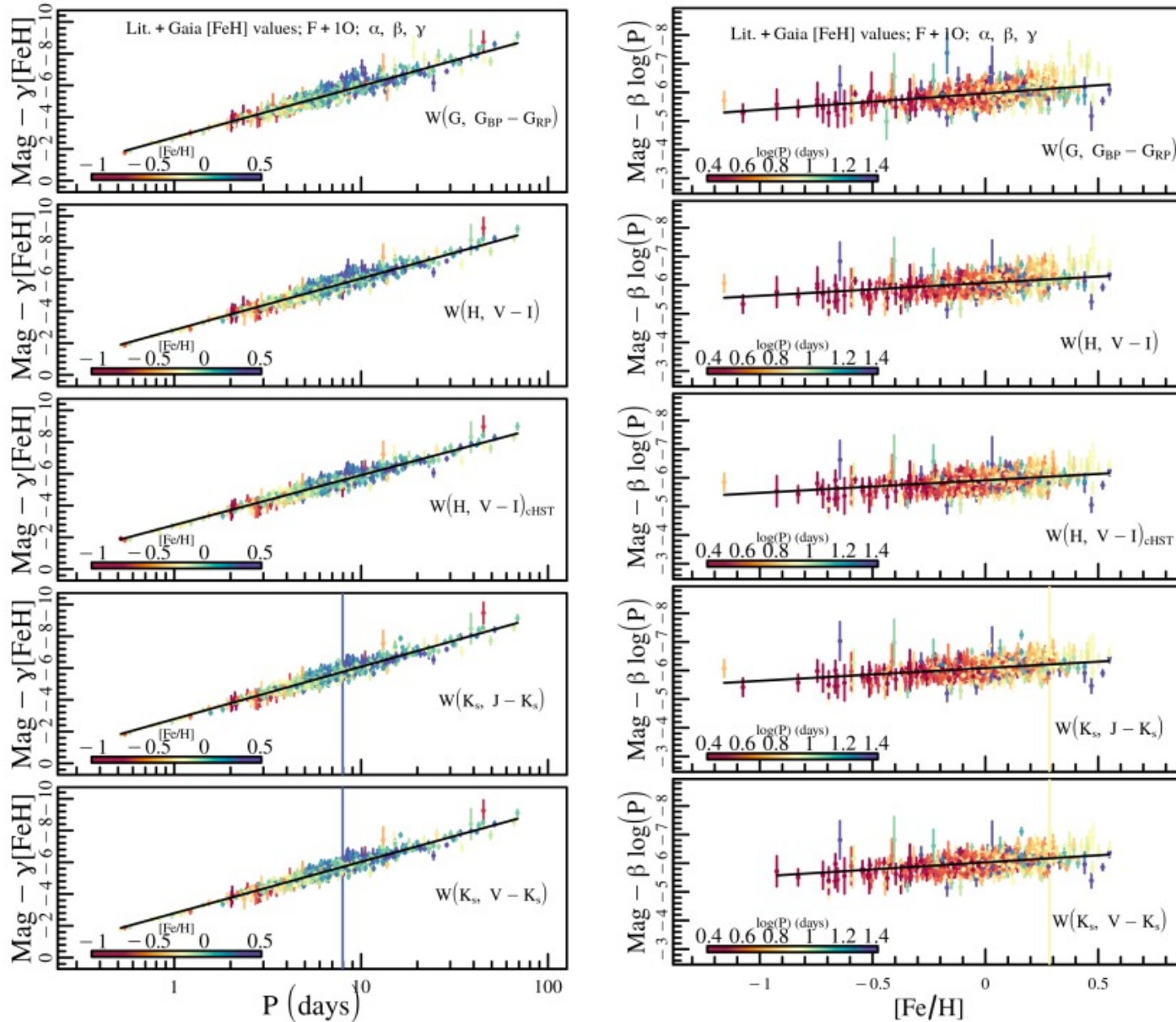
Baseline results: full sample (including Gaia RVS abundances) and F+1O

# Results (Trentin et al. 2024, C-MetaLL IV)

Clear strong trend with  $[\text{Fe}/\text{H}]$  after removing the period dependence.  
Possible flattening at low metallicity

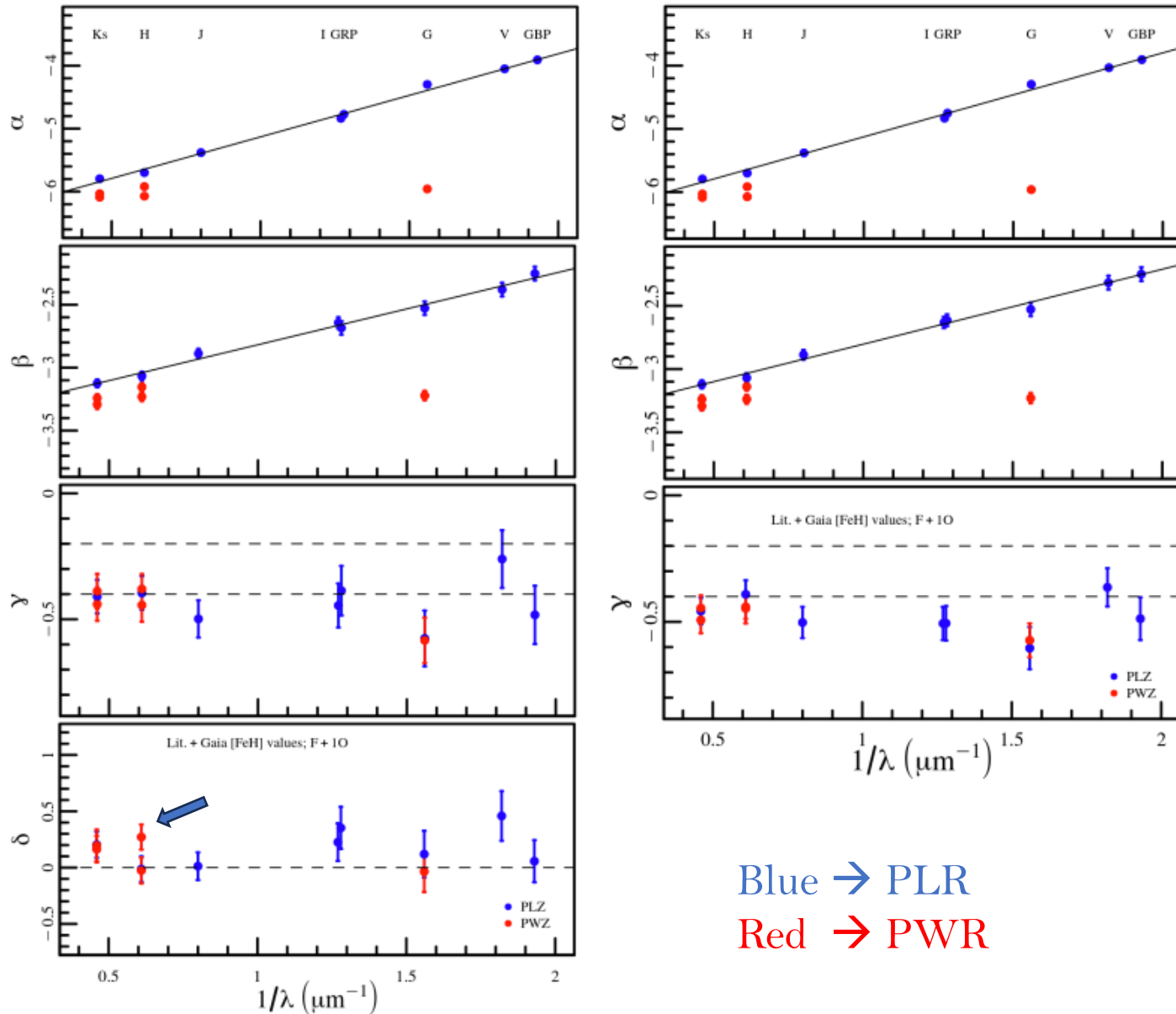


# Results (Trentin et al. 2024, C-MetaLL IV)



Same but for PWZ relations

# Results (Trentin et al. 2024, C-MetaLL IV)



- Baseline solution: HiRes+Gaia, F+10 sample, L21 PZPO, no counter-correction
- $\gamma \sim -0.4$ :  $-0.5$  mag/dex larger than recent results (Gieren+2018, Riess+2021, Breuval+2021,2022)
- No clear metallicity dependence on wavelength for  $\gamma$  term (as in Breuval+2021,2022)
- $\delta$  term significant only in V, I,  $G_{\text{RP}}$  and  $W_{\text{HST}}$  at  $> 1 \sigma \rightarrow$  more data in the metal-poor regime needed to constrain this parameter.

# Test of PLZ relations: different parallax counter-corrections

PL

Counter-correction is anticorrelated with the metallicity effect.

Global ZP = 22  $\mu\text{as}$  (Molinaro et al. 2023)

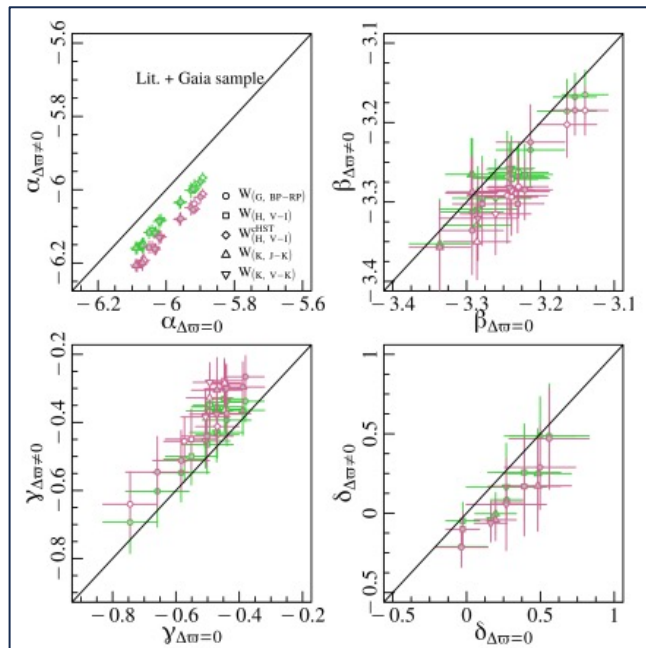
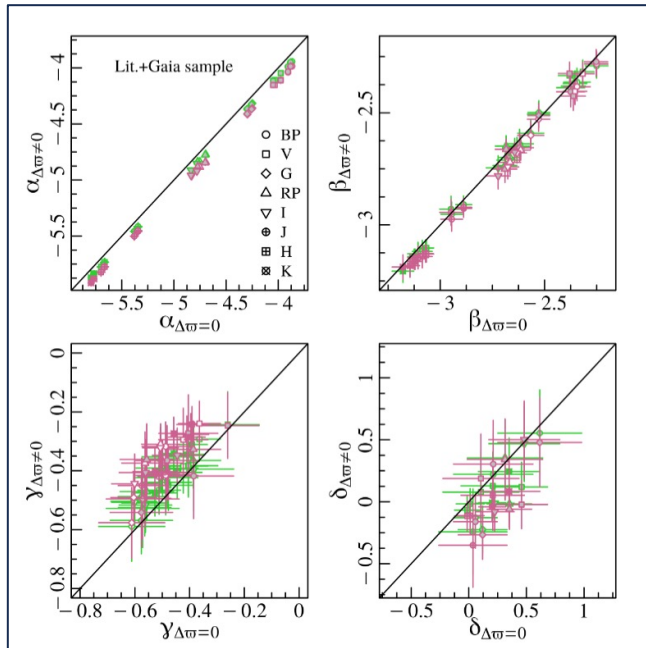
Global ZP = 14  $\mu\text{as}$  (Riess et al. 2021)

If counter-correction increases  $\rightarrow$   $\delta$  unaffected,  $\gamma$  decreases (in absolute value).

Right direction to reconcile our results with recent literature values.

But.....

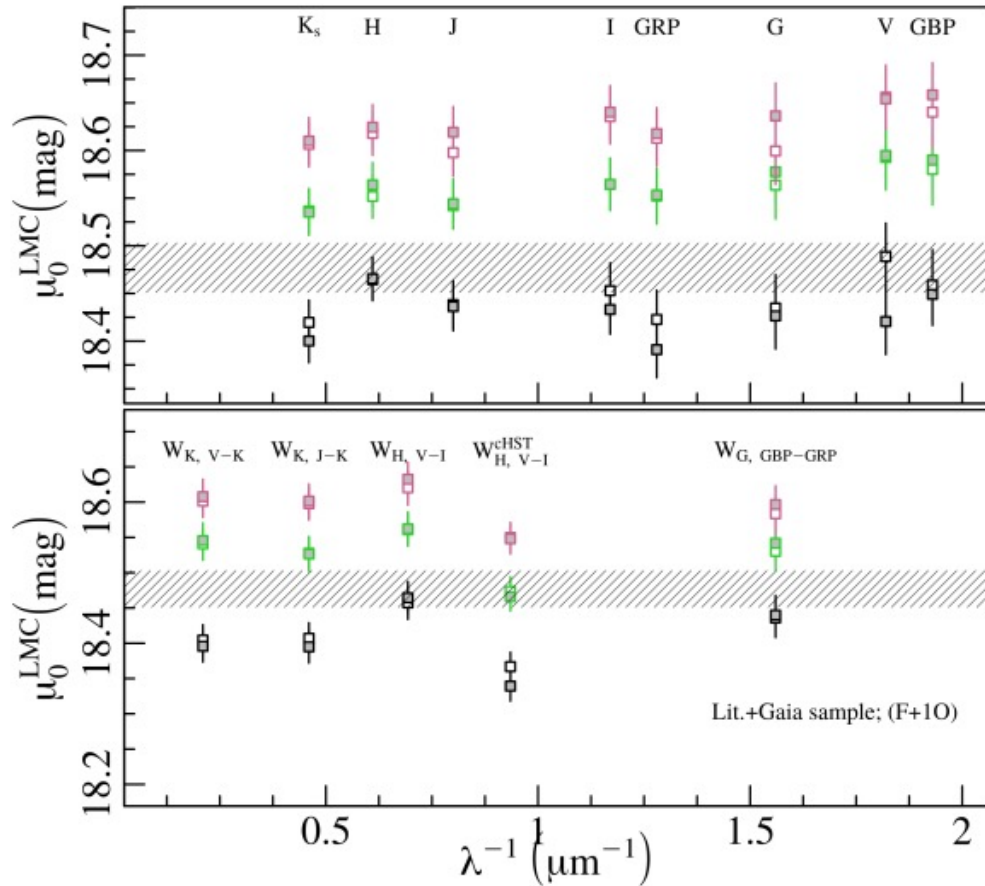
PW





# Test of PLZ relations: different parallax counter-corrections

If we apply our PLZ/PWZ relations to LMC Cepheids (photometry from Gaia/OGLE/VMC, metallicity from Romaniello+2022) and compare the results with the Geometric distances by Pietrzynski+2019 as reference  $\rightarrow$



Counter-correction = 22  $\mu\text{as}$  (Molinaro et al. 2023)

Counter-correction = 14  $\mu\text{as}$  (Riess et al. 2021)

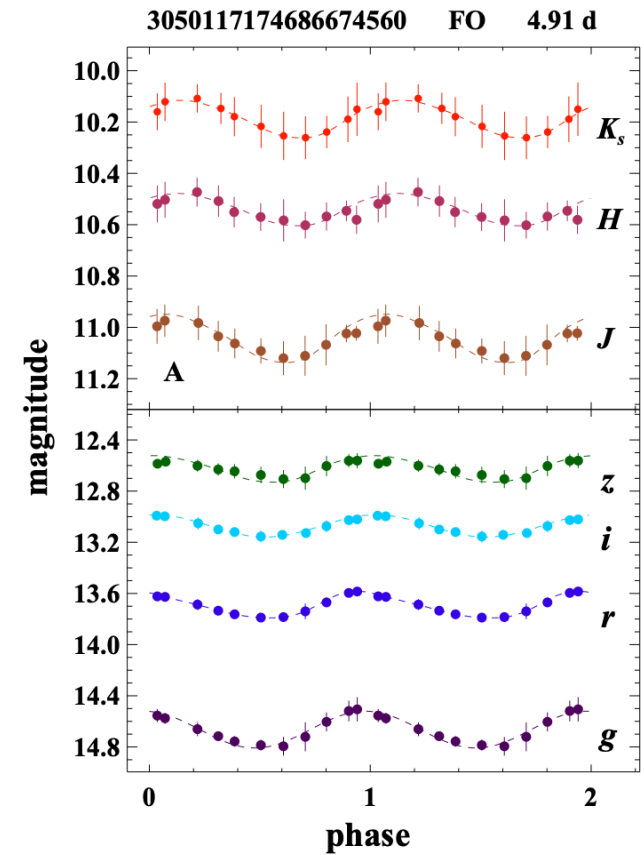
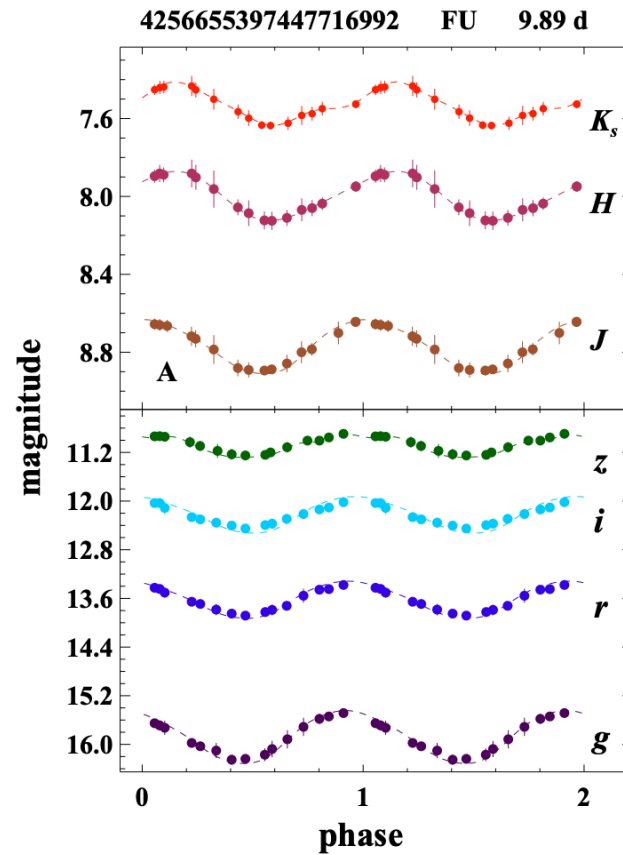
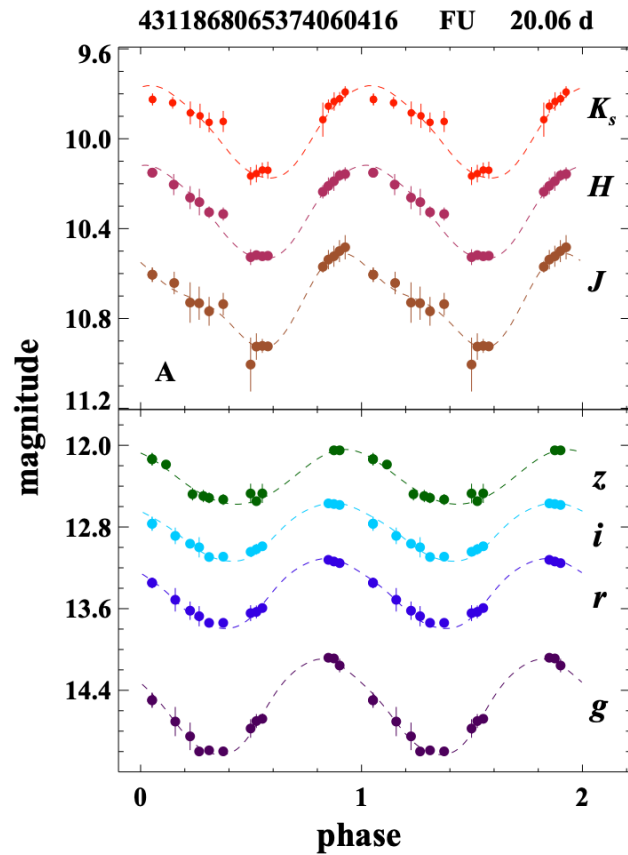
Counter-correction = 0  $\mu\text{as}$

Estimated counter-correction  $\sim 7 \mu\text{as}$

**We can recover the "right" distance of LMC only for  $\gamma \sim -0.4: -0.5$  mag/dex**

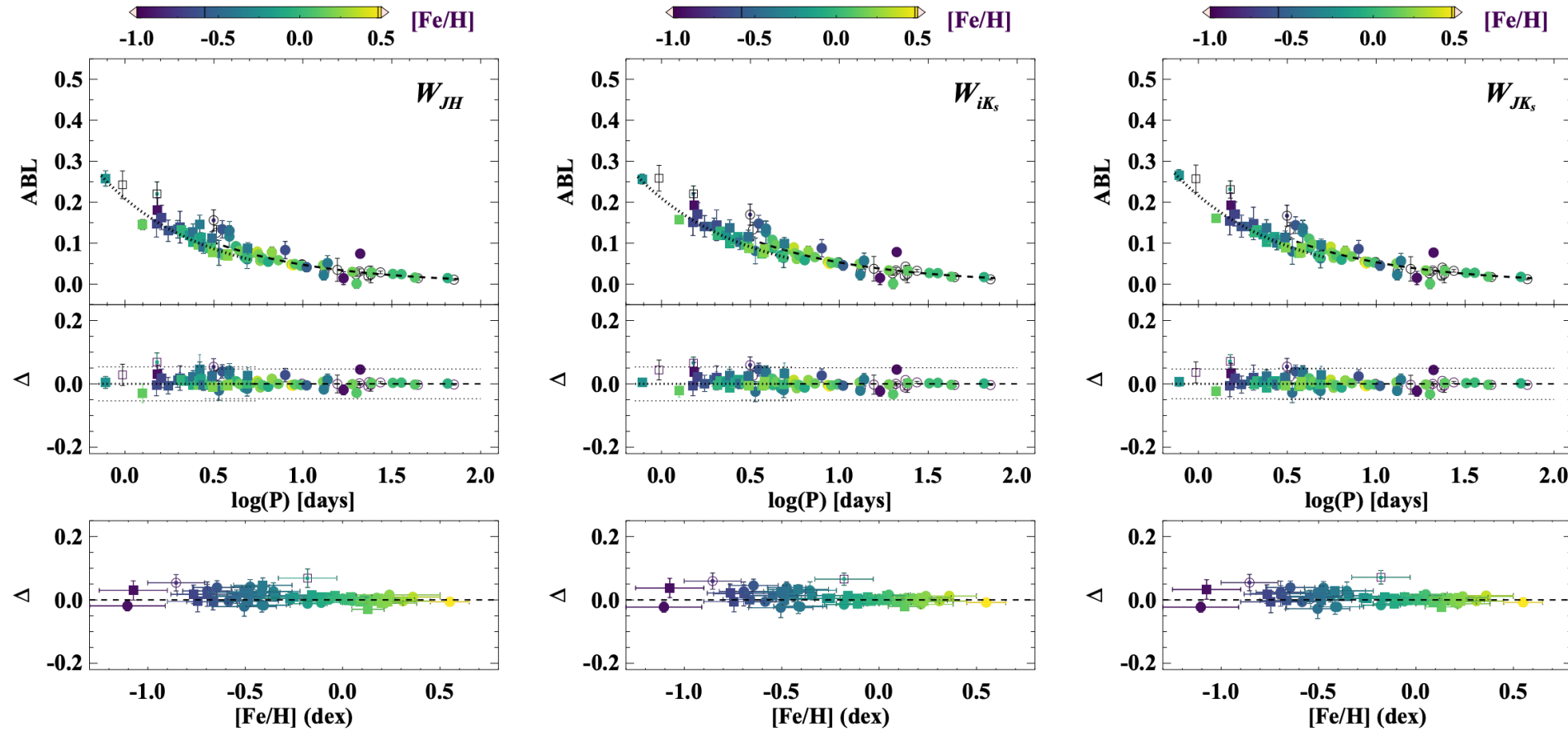
# grizJKs photometry (Bhardwaj et al. 2024, C-MetaLL-V)

Homogeneous optical (griz) and NIR (JHK) photometry of 78 Cepheids (49 F and 29 1O) REM telescope (La Silla, Chile)



# grizJKs photometry (Bhardwaj et al. 2024, C-MetaLL-V)

PL/PW relations derived through ABL fitting  $\rightarrow$  largest residuals with metallicity at low  $[\text{Fe}/\text{H}]$  due to the larger errors in parallax. Need to increase the sample.



# Summary

- Gaia is great but the systematics on the PZPO still impact on the results. Expected a significant reduction of the systematics for DR4, but  $> 2$  years!
- C-MetaLL project:
  1. New calibration of multi-band PLZ/PWZ relations using 910 stars spanning a range of metallicity of 1.5 dex.
  2. For the baseline sample, HiRes+Gaia, F+10:  $\gamma \sim -0.4 : -0.5$  mag/dex  $\rightarrow$  disagreement with the results of the SHOES group.
  3. Hints on a dependence of the slope on the metallicity in the optical bands and in the  $W_{\text{HST}}$  mag (in agreement with theory and other empirical evidences)
  4. Low-metallicity DCEPs have the least precise parallaxes  $\rightarrow$  need to increase the sample to compensate the lower precision.